

Q. No. 2 Part (i) (Page 1)

INVERSE OF FUNCTION

$$\text{Let } f(x) = \frac{3x+2}{2x-1} = y$$

$$\frac{3x+2}{2x-1} = y$$

$$3x+2 = 2xy-y$$

$$3x-2xy = -y-2$$

$$x(3-2y) = -y-2$$

$$x = \frac{-y-2}{(3-2y)}$$

$$\text{As } x = f^{-1}(y) = \frac{-y-2}{3-2y}$$

To Find $f^{-1}(x)$ we replace y by x .

$$f^{-1}(x) = \frac{-x-2}{3-2x}$$

$$f^{-1}(f(x)) = x$$

L.H.S

$$f^{-1}(f(x))$$

$$= f^{-1}\left(\frac{3x+2}{2x-1}\right)$$

$$= \frac{-\frac{3x+2}{2x-1} - 2}{3 - 2\left(\frac{3x+2}{2x-1}\right)}$$

$$= \frac{-\frac{3x+2}{2x-1} - 2}{3 - 2\left(\frac{3x+2}{2x-1}\right)}$$

$$= \frac{-\frac{3x+2}{2x-1} - 2}{3 - 2\left(\frac{3x+2}{2x-1}\right)}$$

$$= \frac{-\frac{3x+2}{2x-1} - 2}{3 - 2\left(\frac{3x+2}{2x-1}\right)}$$

Q. No. 2 Part (i) (Page 2)

$$= \frac{-3x - 2 - 4x + 2}{2x - 1}$$

$$\frac{6x - 3 - 6x - 4}{2x - 1}$$

$$= \frac{-7x}{-7}$$

$$= x$$

$$= \underline{\underline{\text{R.H.S}}}$$

Result

• hence $f^{-1}(x) = \frac{-x-2}{3-2x}$

and $f^{-1}(f(x)) = x$.

Q. No. 2 Part (ii) (Page 1)

$$f(x) = \begin{cases} 3x-1 & x < 1 \\ 4 & x = 1 \\ 2x & x > 1 \end{cases}$$

There are 3 conditions for a continuous function

① $f(c)$ is defined

$$f(1) = 4$$

hence 1st condition is satisfied

② Limit at $x=c$ should exist

For limit to exist, left hand limit = Right hand limit

$$\begin{aligned} \text{Left hand Limit :- } \lim_{x \rightarrow 1^-} f(x) &= \lim_{x \rightarrow 1} (3x-1) \\ &= 3(1)-1 \\ &= 2 \end{aligned}$$

$$\begin{aligned} \text{Right hand Limit :- } \lim_{x \rightarrow 1^+} f(x) &= \lim_{x \rightarrow 1} 2x \\ &= 2(1) \\ &= 2 \end{aligned}$$

L.H.L = R.H.L, so limit exist.

hence 2nd condition is satisfied

③ $f(c) = \lim_{x \rightarrow c} f(x)$

As $f(1) = 4$ and $\lim_{x \rightarrow 1} f(x) = 2$, 3rd condition is not satisfied. So $f(x)$ is discontinuous at $x=1$.

Q. No. 2 Part (ii) (Page 2)

Result

function is discontinuous at $x=1$.

Q. No. 2 Part (iii) (Page 1)

GIVEN:

$$y = \cot(q \cot^{-1} u)$$

TO PROVE:

$$(1+u^2)y_1 - q(1+y^2) = 0.$$

PROOF:

$$\text{As } y = \cot(q \cot^{-1} u)$$

$$\cot^{-1} y = q \cot^{-1} u$$

Differentiating both sides:

$$\frac{d}{du} \cot^{-1} y = q \frac{d}{du} \cot^{-1} u$$

$$\frac{-1}{1+y^2} \frac{dy}{du} = q \frac{-1}{1+u^2}$$

$$\frac{dy}{du} \left(\frac{1}{1+y^2} \right) = \frac{q}{1+u^2}$$

$$(1+u^2) \frac{dy}{du} = q(1+y^2)$$

$$(1+u^2) \frac{dy}{du} - q(1+y^2) = 0$$

$$(1+u^2)y_1 - q(1+y^2) = 0$$

hence proved

RESULT:

If $y = \cot(q \cot^{-1} u)$ then $(1+u^2)y_1 - q(1+y^2) = 0.$

Q. No. 2 Part (iii) (Page 2)

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Q. No. 2 Part (iv) (Page 1)

Approximate value of $\sin 61^\circ$.

By Taylor series:-

$$f(x+h) = f(x) + f'(x)h + \frac{f''(x)h^2}{2} + \frac{f'''(x)h^3}{6} + \dots$$

Let $f(x) = \sin x$ $x = 60^\circ$ and $h = 1^\circ = 0.01745$

$$f(x) = \sin x$$

$$f'(x) = \cos x$$

$$f''(x) = -\sin x$$

$$f'''(x) = -\cos x$$

So:-

$$f(x+h) = f(x) + f'(x)h + \frac{f''(x)h^2}{2} + \frac{f'''(x)h^3}{6} + \dots$$

$$\sin(x+h) = \sin x + \cos x \cdot h + \frac{h^2}{2} (-\sin x) + \frac{h^3}{6} (-\cos x) + \dots$$

put $x = 60^\circ$, $h = 0.01745 = 1^\circ$

$$\sin(60+1) = \sin 60 + (\cos 60)(0.01745) + \frac{(0.01745)^2}{2} (-\sin 60) - \frac{\cos 60}{6} (0.01745)^3 + \dots$$

$$= \frac{\sqrt{3}}{2} + \frac{1}{2}(0.01745) - \frac{\sqrt{3}}{2 \times 2} (0.01745)^2 - \frac{1}{2 \times 6} (0.01745)^3 + \dots$$

$$= 0.874618$$

SEE NEXT PAGE
(Pg 10)

Q. No. 2 Part (iv) (Page 2) USING DIFFERENTIALS:-

$$\text{Let } f(x) = \sin x$$

$$\text{As } f(x+\delta x) \approx f(x) + dy$$

$$f(x+\delta x) \approx f(x) + f'(x) \cdot dx \rightarrow \textcircled{1}$$

• $f(x) = \sin x$ with $x = 60^\circ$, $dx = 1^\circ = 0.01745$

$$\text{At } x = 60^\circ, \sin 60 = \frac{\sqrt{3}}{2}$$

• $dy = f'(x) \cdot dx$
 $= \cos x \cdot (0.01745)$
 $= \cos 60 \times 0.01745$
 $= 8.7225 \times 10^{-3}$

putting value of $f(x)$ and dy in $\textcircled{1}$, we get:-

$$\begin{aligned} \sin(60+1) &\approx \sin 60 + dy \\ &\approx 0.866 + 8.7225 \times 10^{-3} \\ &\approx 0.874725 \end{aligned}$$

RESULT

hence by using differentials, approximate value of $\sin 61 = 0.874725$.

Q. No. 2 Part (v) (Page 1)

AREA UNDER CURVE

$$y = x^3 - 9x$$

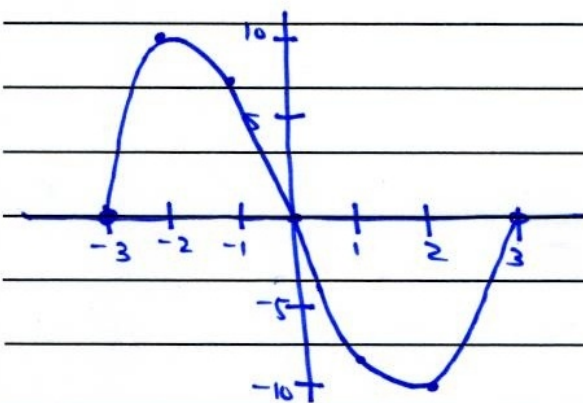
For x intercept; put $y = 0$

$$0 = x(x^2 - 9)$$

$$x = 0 \text{ or } x^2 - 9 = 0$$

$$x = \pm 3$$

so intervals are $[-3, 0]$ and $[0, 3]$



$$x = -3 \Rightarrow y = 0$$

$$x = -2 \Rightarrow y = 10$$

$$x = -1 \Rightarrow y = 8$$

$$x = 0 \Rightarrow y = 0$$

$$x = 1 \Rightarrow y = -8$$

$$x = 2 \Rightarrow y = -10$$

$$x = 3 \Rightarrow y = 0$$

To find area under curve:-

$$A = \int_{-3}^0 (x^3 - 9x) \cdot dx - \int_0^3 (x^3 - 9x) \cdot dx$$

$$= \left| \frac{x^4}{4} - \frac{9}{2}x^2 \right|_{-3}^0 - \left| \frac{x^4}{4} - \frac{9}{2}x^2 \right|_0^3$$

$$= \frac{(0 - (-3)^4)}{4} - \frac{9}{2}(0 - (-3)^2) - \left(\frac{(3)^4}{4} - 0 \right) + \frac{9}{2}(9 - 0)$$

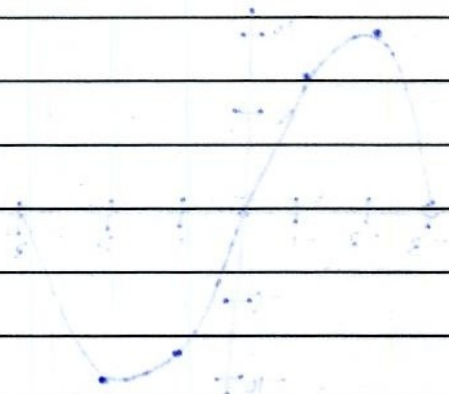
$$= \frac{-81}{4} - \frac{9}{2}(-9) - \frac{81}{4} + \frac{81}{2}$$

$$= \frac{81}{2} \text{ square units}$$

Q. No. 2 Part (v) (Page 2)

RESULT

• hence area under curve is $\frac{81}{2}$ sq units.



Q. No. 2 Part (vi) (Page 1)

$$\frac{dy}{du} = \frac{3}{4}u^3 + u - 3$$

$$dy = \left(\frac{3}{4}u^3 + u - 3\right) \cdot dx$$

integrating both sides, we have:-

$$\int dy = \frac{3}{4} \int u^3 dx + \int x \cdot dx - 3 \int 1 dx$$

$$y = \frac{3x^4}{4 \times 4} + \frac{x^2}{2} - 3x + C$$

$$y = \frac{3x^4}{16} + \frac{x^2}{2} - 3x + C \rightarrow \textcircled{1}$$

Applying initial condition:-

$$y = 0 \text{ when } u = 2$$

$$0 = \frac{3(2^4)}{16} + \frac{4}{2} - 3(2) + C$$

$$0 = 3 + 2 - 6 + C$$

$$0 = -1 + C$$

$$C = 1$$

put in $\textcircled{1}$:-

$$y = \frac{3x^4}{16} + \frac{x^2}{2} - 3x + 1$$

RESULT

- hence $y = \frac{3x^4}{16} + \frac{x^2}{2} - 3x + 1$ is solution of given differential equation.

Q. No. 2 Part (vi) (Page 2)

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Q. No. 2 Part (vii) (Page 1)

NORMAL FORM OF EQUATION:-

$$x \cos \alpha + y \sin \alpha = p$$

put $\alpha = 30^\circ$ & $p = 8$.

$$\frac{\sqrt{3}}{2}x + \frac{1}{2}y = 8$$

$$\frac{1}{2}y = -\frac{\sqrt{3}}{2}x + 8$$

$$y = -\sqrt{3}x + 16 \rightarrow \textcircled{1}$$

comparing with slope intercept form:-

$$y = mx + c$$

$$m = -\sqrt{3} \quad ; \quad c = 16$$

RESULTslope of line is $-\sqrt{3}$ and y intercept is 16.

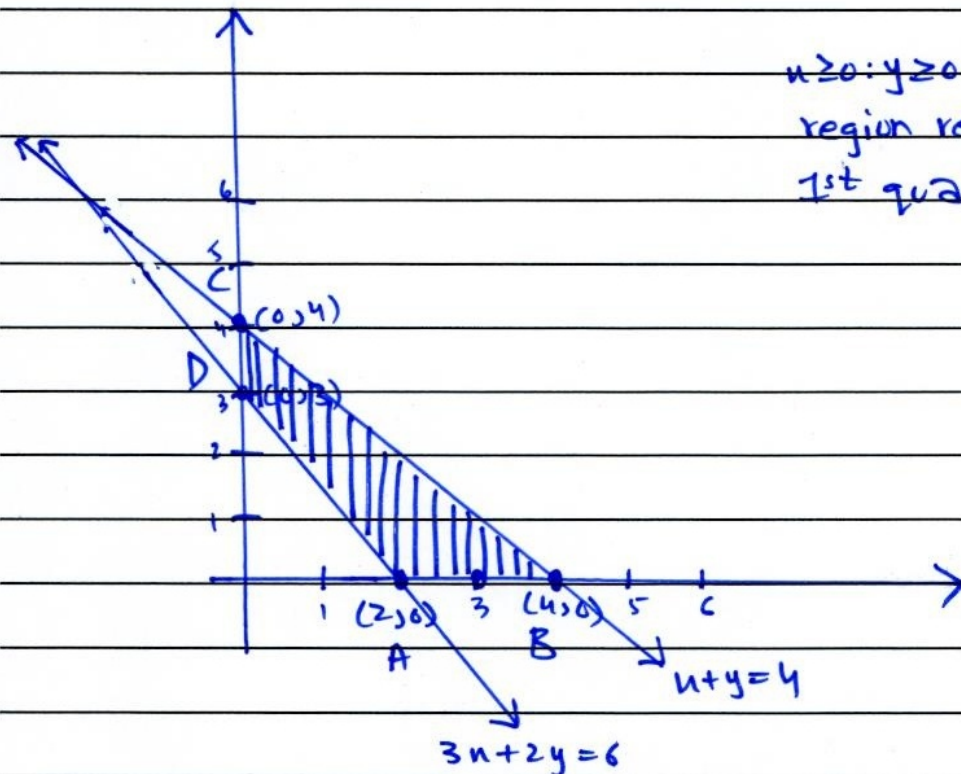
(Section B)

Q. No. 2 Part (vii) (Page 2)

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Q. No. 2 Part (viii) (Page 1)

ASSOCIATED EQUATIONS	$3x+2y=6$	$x+y=4$	$x \geq 0; y \geq 0$
INTERCEPTS	$\frac{x}{2} + \frac{y}{3} = 1$ $(2,0) (0,3)$	$\frac{x}{4} + \frac{y}{4} = 1$ $(4,0) (0,4)$	
INEQUALITIES	$3x+2y > 6$	$x+y < 4$	
TEST POINT $(0,0)$	$0+0 > 6$ False	$0+0 < 4$ TRUE	
SOLUTION REGION	lies away from $(0,0)$	lies toward $(0,0)$	



$x \geq 0; y \geq 0$ mean solution region restricted to 1st quadrant.

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GRAPH ON GRAPH SHEET AS WELL.

Q. No. 2 Part (viii) (Page 2)

∴ CORNER POINTS are

1) $A(2,0)$

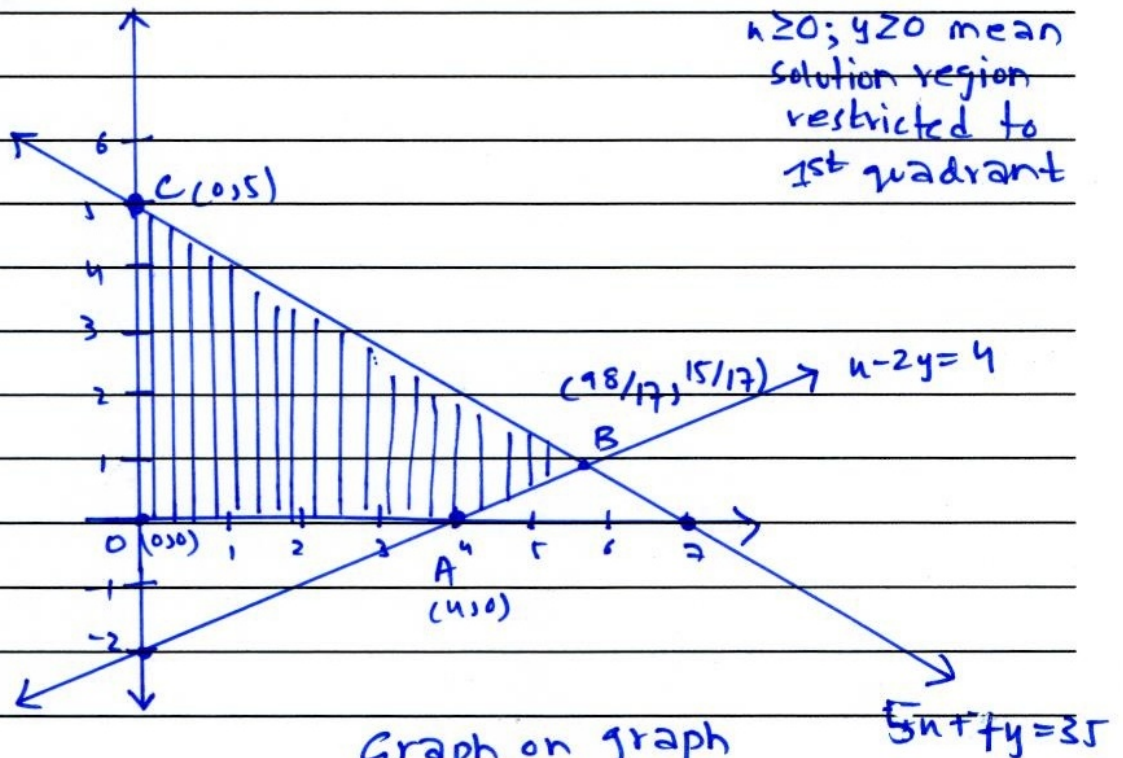
2) $B(4,0)$

3) $C(0,4)$

4) $D(0,3)$

Q. No. 2 Part (ix) (Page 1)

ASSOCIATED EQUATIONS	$5x + 7y = 35$	$x - 2y = 4$	$x \geq 0, y \geq 0$
INTERCEPTS	$\frac{x}{7} + \frac{y}{5} = 1$ (7,0) (0,5)	$\frac{x}{4} - \frac{y}{2} = 1$ (4,0) (0,-2)	
INEQUALITIES	$5x + 7y < 35$	$x - 2y < 4$	
TEST POINT (0,0)	$0 + 0 < 35$ TRUE	$0 - 0 < 4$ TRUE	
SOLUTION REGION	lies toward (0,0)	lies toward (0,0)	



Graph on graph sheet as well
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Q. No. 2 Part (ix) (Page 2)

∴ CORNER POINTS ARE:-

1) O (0,0)

2) A (4,0)

3) B ($\frac{98}{17}, \frac{15}{17}$)

4) C (0,5)

$$\begin{aligned} \therefore 5x + 7y &= 35 \\ + 8x + 10y &= 20 \end{aligned}$$

$$17y = 15$$

$$y = \frac{15}{17}$$

$$x = \frac{98}{17}$$

Q. No. 2 Part (x) (Page 1) **VALUE OF c**

$$5x + 2y + c = 0$$

$$m = \frac{-5}{2}$$

$$\frac{x^2}{4} - \frac{y^2}{9} = 1.$$

$$a^2 = 4 \quad b^2 = 9$$

c for this type of hyperbola is given as:-

$$c = \sqrt{a^2 m^2 - b^2}$$

$$c = \sqrt{\left(\frac{25}{4}\right) \cdot 4 - 9}$$

$$c = \sqrt{16}$$

$$c = \pm 4.$$

RESULT

- $5x + 2y + c = 0$ will touch the hyperbola if $c = \pm 4$

(Section B)

Q. No. 2 Part (x) (Page 2)

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Q. No. 2 Part (xi) (Page 1)

POINT OF INTERSECTION:-

$$\frac{x^2}{18} + \frac{y^2}{8} = 1 \rightarrow (1); \quad \frac{x^2}{3} - \frac{y^2}{3} = 1 \rightarrow (2)$$

Multiply eq (2) with $\frac{1}{6}$ and subtract from (1).

$$\frac{x^2}{18} + \frac{y^2}{8} = 1$$

$$- \frac{x^2}{18} + \frac{y^2}{18} = \frac{1}{6}$$

$$\frac{y^2}{8} + \frac{y^2}{18} = 1 - \frac{1}{6}$$

$$\frac{13y^2}{72} = \frac{5}{6}$$

$$13y^2 = 12 \times 5$$

$$13y^2 = 60.$$

$$y^2 = \frac{60}{13}$$

$$y = \pm \sqrt{\frac{60}{13}}$$

put in (1) :-

$$\frac{x^2}{18} + \frac{\left(\frac{60}{13}\right)}{8} = 1$$

$$\frac{x^2}{18} = 1 - \frac{15}{26}$$

$$x^2 = 18 \times \frac{11}{26}$$

$$x = \pm \sqrt{\frac{99}{13}}$$

Q. No. 2 Part (xi) (Page 2)

RESULT

Hence there are 4 point of intersection:

1) $\left(\sqrt{\frac{99}{13}}, \sqrt{\frac{60}{13}}\right)$

2) $\left(\sqrt{\frac{99}{13}}, -\sqrt{\frac{60}{13}}\right)$

3) $\left(-\sqrt{\frac{99}{13}}, \sqrt{\frac{60}{13}}\right)$

4) $\left(-\sqrt{\frac{99}{13}}, -\sqrt{\frac{60}{13}}\right)$

Q. No. 2 Part (xii) (Page 1)

MOMENT OF FORCE :-

$$J = \vec{r} \times \vec{F}$$

$$\vec{F}_{\text{net}} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3$$

$$= (\underline{i} - 2\underline{j}) + (3\underline{i} + 2\underline{j} - \underline{k}) + (5\underline{j} + 2\underline{k})$$

$$= 4\underline{i} + 5\underline{j} + \underline{k}$$

$$\vec{r} = (\text{About Point}) - (\text{Point of application})$$

$$= (2, 0, 1) - (1, 1, 1)$$

$$= (1, -1, 0)$$

$$J = \vec{r} \times \vec{F}$$

$$= \begin{vmatrix} \underline{i} & \underline{j} & \underline{k} \\ 1 & -1 & 0 \\ 4 & 5 & 1 \end{vmatrix}$$

$$= \underline{i}(-1) - \underline{j}(1) + \underline{k}(5+4)$$

$$= -\underline{i} - \underline{j} + 9\underline{k}$$

$$\text{Magnitude} = \sqrt{1+1+81} = \sqrt{83}$$

RESULT

→ Moment of force is $-\underline{j} - \underline{i} + 9\underline{k}$ with magnitude $= \sqrt{83}$

Q. No. 2 Part (xii) (Page 2)

MOMENT OF FORCE IS

It is the product of force and perpendicular distance from the point of rotation to the line of action of the force.

It is denoted by M and its SI unit is Nm .

It is a vector quantity and its direction is given by the right hand rule.

It is denoted by $M = F \times d$.

It is a scalar quantity.

RESULT

The moment of force is a vector quantity and its direction is given by the right hand rule.

Q. No. 3 (Page 1)

APPLICATION OF EXTREME VALUES:Let length of square base = x , height = h .

GIVEN:-

$$V = x^2 h$$

$$32 = x^2 h$$

$$h = \frac{32}{x^2} \rightarrow (1)$$

As surface of box will be:-

$$A = x^2 + 4hx$$

putting value of h from (1).

$$A = x^2 + 4\left(\frac{32}{x^2}\right)x$$

$$A = x^2 + \frac{128}{x}$$

Let $A = f(x)$, so

$$f'(x) = 2x - \frac{128}{x^2} \rightarrow (2)$$

$$f''(x) = 2 + \frac{256}{x^3} \rightarrow (3)$$

For stationary point:- we take $f'(x) = 0$

$$f'(x) = 2x - \frac{128}{x^2}$$

$$0 = 2x - \frac{128}{x^2}$$

$$\frac{128}{x^2} = 2x$$

$$64 = x^3$$

$$\Rightarrow x = 4$$

put $x = 4$ in (3)

Q. No. 3 (Page 2)

$$f''(x) = 2 + \frac{256}{x^3}$$

$$f''(4) = 2 + \frac{256}{64} = 6$$

As $f''(4) = 6 > 0$, hence $x=4$ leads to a minimum value.

$$\text{Thus } h = \frac{32}{x^2} = \frac{32}{(4)^2} = \frac{32}{16} = 2$$

Result

Thus for least material requirements, length of square base of box will be 4 and height will be 2

Q. No. 4 (Page 1)

EQUATION OF TANGENT

We have to find equation of tangent that are parallel to $3x+8y+1=0$.

- \rightarrow slope of this line = $-\frac{3}{8}$
- \rightarrow slope of tangents = $-\frac{3}{8}$

$$\frac{x^2}{128} + \frac{y^2}{18} = 1$$

Ellipse is of the form: $-\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$
where $a^2=128, b^2=18$

Equation of tangent to ellipse is:-

$$y = mx \pm \sqrt{a^2 m^2 + b^2}$$

put value of m, a^2, b^2

$$y = \frac{-3}{8}x \pm \sqrt{\frac{128 \cdot 9}{64} + 18}$$

$$y = \frac{-3}{8}x \pm \sqrt{18+18}$$

$$y = \frac{-3}{8}x \pm \sqrt{36}$$

$$y = \frac{-3}{8}x \pm 6$$

$$8y = -3x \pm 6$$

$$3x + 8y \pm 6 = 0$$

Result

Required equation of tangents are $3x+8y \pm 6=0$

Q. No. 4 (Page 2)

POINT OF CONTACT

$$3u + 8y + 1 = 0$$

$$3u = -1 - 8y$$

$$u = \frac{-1 - 8y}{3} \rightarrow \textcircled{1}$$

put $u = \frac{-1 - 8y}{3}$ in equation of ellipse :-

$$\frac{x^2}{128} + \frac{y^2}{18} = 1$$

$$\frac{(-1 - 8y)^2}{1 \times 128} + \frac{y^2}{18} = 1$$

$$\frac{64y^2 + 16y + 1}{1152} + \frac{y^2 \times 64}{18 \times 64} = 1$$

$$64y^2 + 16y + 1 + 64y^2 = 1152$$

$$128y^2 + 16y - 1151 = 0$$

$$y = 2.93$$

$$u = -8.14$$

$$y = -3.06$$

$$u = 7.82$$

Thus point of contacts are $(-8.14, 2.93)$ and $(7.82, -3.06)$

Q. No. 4 (Page 4)



Q. No. 5 (Page 1) $A(-3, -4)$ $B(4, 6)$ $C(4, -3)$

A)

Equation of side AB:-

$$\frac{y - y_1}{y_2 - y_1} = \frac{x - x_1}{x_2 - x_1}$$

$$\frac{y + 4}{6 + 4} = \frac{x + 3}{4 + 3}$$

$$\frac{y + 4}{10} = \frac{x + 3}{7}$$

$$7y + 28 = 10x + 30$$

$$10x - 7y + 2 = 0$$

Equation of side AC:-

$$\frac{y - y_1}{y_2 - y_1} = \frac{x - x_1}{x_2 - x_1}$$

$$\frac{y + 4}{-3 + 4} = \frac{x + 3}{4 + 3}$$

$$\frac{y + 4}{1} = \frac{x + 3}{7}$$

$$7y + 28 = x + 3$$

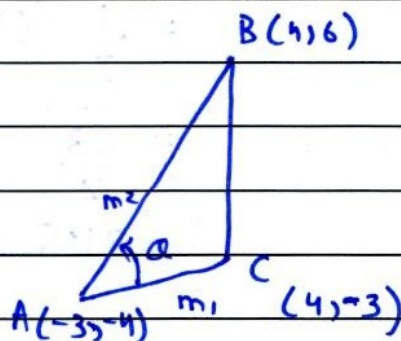
$$x - 7y - 25 = 0$$

B)

$$\text{slope of AB} = m_2 = \frac{10}{7}$$

$$\text{slope of AC} = m_1 = \frac{1}{7}$$

$$\tan \theta = \frac{m_2 - m_1}{1 + m_1 m_2}$$



Q. No. 5 (Page 2)

$$\tan \theta = \frac{\frac{10}{7} - \frac{1}{7}}{1 + \left(\frac{10}{7}\right)\left(\frac{1}{7}\right)}$$

$$\tan \theta = \frac{\frac{9}{7}}{\frac{49+10}{49}} = \frac{\frac{9}{7}}{\frac{59}{49}} = \frac{9 \times 7}{59} = \frac{63}{59}$$

$$\theta = \tan^{-1}\left(\frac{63}{59}\right)$$

$$\theta = 46.8^\circ$$

c)

$$\text{Area of } \Delta = \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$$

$$\text{Area of } \Delta ABC = \frac{1}{2} \begin{vmatrix} 4 & 6 & 1 \\ -3 & -4 & 1 \\ 4 & -3 & 1 \end{vmatrix}$$

$$= \frac{1}{2} [4(-4+3) - 6(-3-4) + 1(9+16)]$$

$$= \frac{1}{2} (63)$$

$$= \frac{63}{2}$$

$$= 31.5 \text{ square units}$$

hence area of ΔABC is $\frac{63}{2}$ sq units.

Q. No. 5 (Page 3)

D)

perpendicular distance from C to \overline{AB} .

$$d = \frac{|ax_1 + by_1 + c|}{\sqrt{a^2 + b^2}}$$

So distance of C from \overline{AB} is:-

$$\overline{AB} \text{ equation :- } 10x - 7y + 2 = 0$$

$$d = \frac{|10(4) + (-7)(-3) + 2|}{\sqrt{10^2 + 7^2}}$$

$$d = \frac{40 + 21 + 2}{\sqrt{149}}$$

$$d = \frac{63}{\sqrt{149}}$$

hence distance of C from \overline{AB} is $\frac{63}{\sqrt{149}}$ units.

Q. No. 5 (Page 4)

(1)

20) A person is standing at a distance of 100 m from a wall. He is holding a gun. The sound of the gun is heard by him after 0.5 s. Calculate the speed of sound.

Given: Distance = 100 m, Time = 0.5 s

Formula: $\text{Speed} = \frac{\text{Distance}}{\text{Time}}$

Solution: $\text{Speed} = \frac{100 \text{ m}}{0.5 \text{ s}} = 200 \text{ m/s}$

Q. No. 6 (Page 1)

ELEMENTS OF CONIC

$$9x^2 - y^2 - 12x - 2y + 2 = 0$$

$$9\left(x^2 - \frac{12}{9}x\right) - (y^2 + 2y) + 2 = 0$$

$$9\left(x^2 - 2\left(\frac{6}{9}\right) + \frac{36}{9}\right) - \frac{y^2 + 2y + 1}{9} - (y^2 + 2y + 1) + 1 + 2 = 0$$

$$9\left(x - \frac{2}{3}\right)^2 + 3 - 4 - (y + 1)^2 = 0$$

$$9\left(x - \frac{2}{3}\right)^2 - (y + 1)^2 = 4 - 3$$

$$9\left(x - \frac{2}{3}\right)^2 - (y + 1)^2 = 1$$

$$\frac{\left(x - \frac{2}{3}\right)^2}{\frac{1}{9}} - (y + 1)^2 = 1 \rightarrow \textcircled{1}$$

Let $x - \frac{2}{3} = X$ and $y + 1 = Y$

So equation (1) becomes:-

$$\frac{X^2}{\frac{1}{9}} - Y^2 = 1 \rightarrow \textcircled{2}$$

$$a^2 = \frac{1}{9} ; b^2 = 1$$

In hyperbola :- $c^2 = a^2 + b^2$

$$c^2 = 1 + \frac{1}{9} = \frac{10}{9}$$

$$c = \pm \frac{\sqrt{10}}{3}$$

$$a = \pm \frac{1}{3} , b = \pm 1$$

Q. No. 6 (Page 2)

centre

centre of (2) is:-

$$X=0$$

$$Y=0$$

$$x - \frac{2}{3} = 0$$

$$y + 1 = 0$$

$$x = \frac{2}{3}$$

$$y = -1$$

Thus centre of hyperbola is $(\frac{2}{3}, -1)$

Focii

Focii of (2) is:-

$$X = \pm c$$

$$Y = 0$$

$$x - \frac{2}{3} = \pm \frac{\sqrt{10}}{3}$$

$$y + 1 = 0$$

$$y = -1$$

$$x = \frac{2 \pm \sqrt{10}}{3}$$

$$x = \frac{2 \pm \sqrt{10}}{3}$$

Thus focii of hyperbola are $(\frac{2 \pm \sqrt{10}}{3}, -1)$

Eccentricity

eccentricity $e = \frac{c}{a}$

$$e = \frac{\sqrt{10}}{\frac{1}{3}}$$

$$e = \sqrt{10}$$

vertices

vertices of (2) are:-

$$X = \pm a$$

$$Y = 0$$

$$x - \frac{2}{3} = \pm \frac{1}{3}$$

$$y + 1 = 0$$

$$x = \frac{2 \pm 1}{3}$$

$$y = -1$$

Q. No. 6 (Page 3)

$$e = \frac{2+1}{3} = \frac{3}{3} = 1$$

OR

$$e = \frac{2-1}{3} = \frac{1}{3}$$

Thus vertices of hyperbola are $(\frac{1}{3}, -1)$ and $(1, -1)$

Directrices

$$X = \pm \frac{a}{e}$$

$$e = \frac{2}{3} = \pm \frac{1}{\sqrt{10}}$$

$$e = \frac{2}{3} \pm \frac{1}{3\sqrt{10}}$$

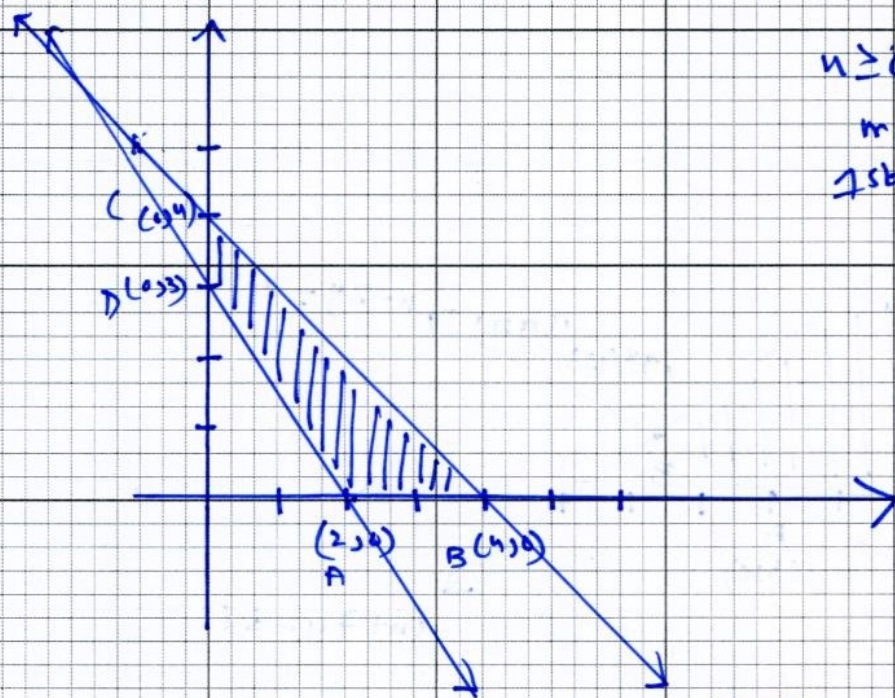
Thus directrices of hyperbola are $e = \frac{2}{3} \pm \frac{1}{3\sqrt{10}}$

Q. No. 6 (Page 4)

[Faint, illegible handwriting is visible on the page, appearing to be bleed-through from the reverse side. Some words like "Directives" and "The" are partially discernible.]



Q2 (viii)



$$x \geq 0, y \geq 0$$

mean
1st Quadrant

$$3x + 2y = 6$$

$$x + y = 4$$

A (2,0)

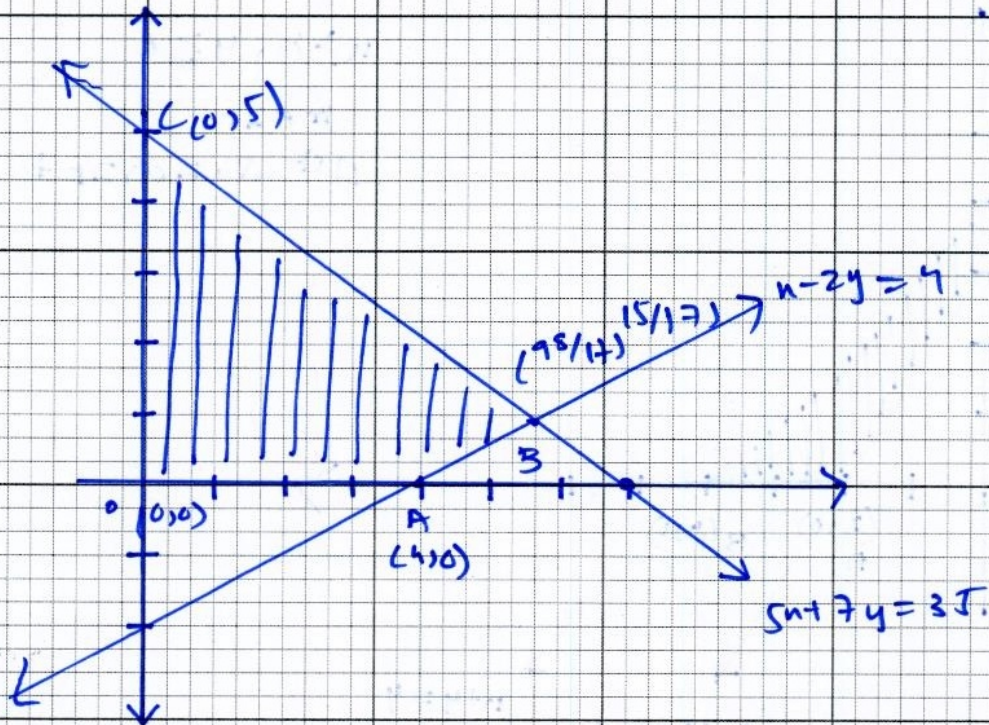
B (4,0)

D (0,3)

C (0,4)

Q2(i x)

$x \geq 0$ $y \geq 0$
mean 1st quadrant



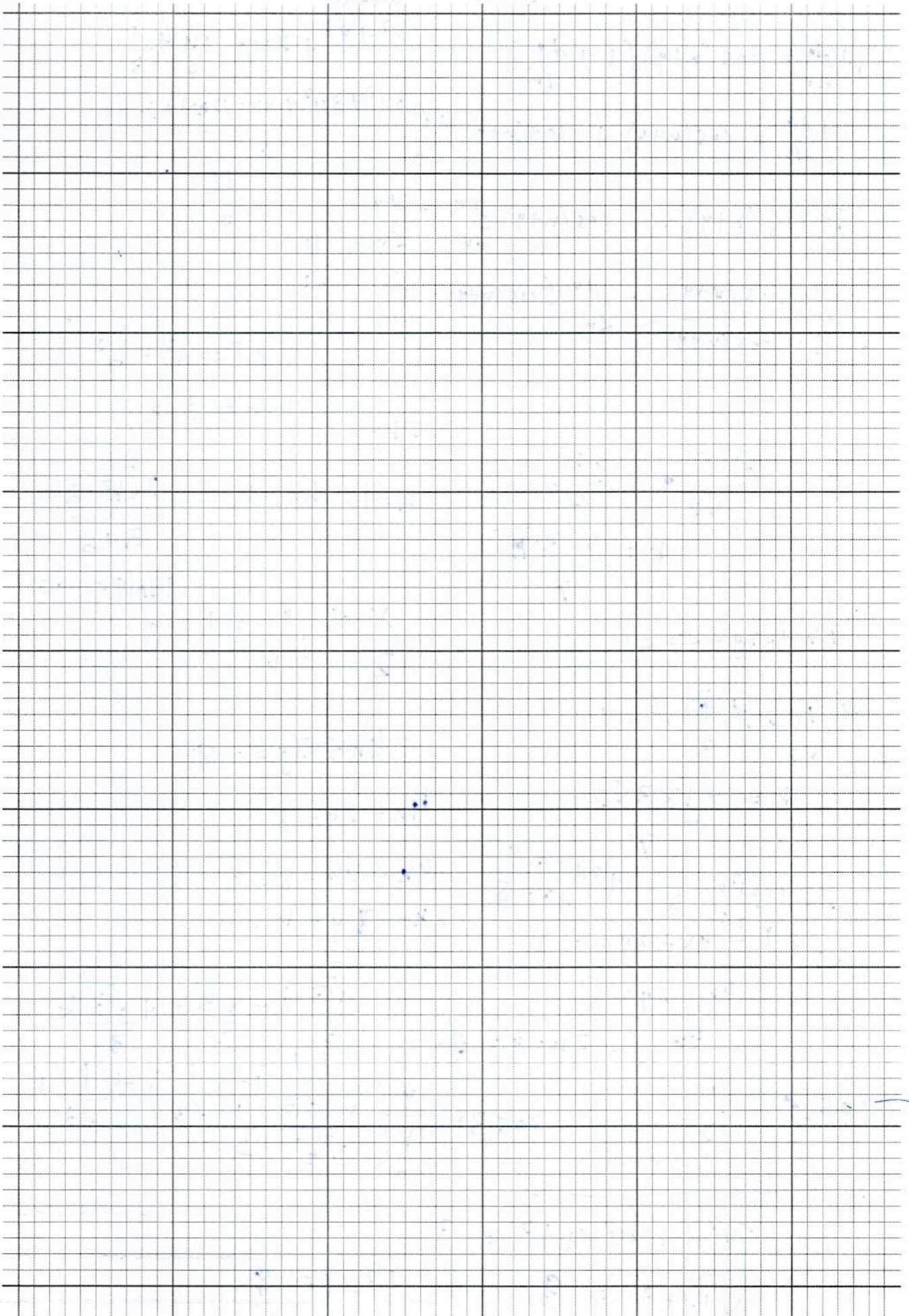
$$O(0,0)$$

$$A(4,0)$$

$$B(\frac{98}{17}, \frac{15}{17})$$

$$C(0,5)$$

Graph Page No. 1



$$1 + \frac{dy}{dx} = \cos(x+y) \left(1 + \frac{dy}{dx}\right)$$

$$1 + \frac{dy}{dx} = \cos(x+y) + \cos(x+y) \frac{dy}{dx}$$

$$1 - \cos(x+y) = \cos(x+y) \frac{dy}{dx} - \frac{dy}{dx}$$

$$\frac{1 - \cos(x+y)}{-(1 - \cos(x+y))} = \frac{dy}{dx} (\cancel{\cos(x+y)} - 1)$$

$$x^2 + y^2 + 2x - 4y + \frac{1}{3}$$

$$3x^2 + 3y^2 + 6x - 12y + 1$$

$$4 \frac{16}{3}$$

$$\frac{4}{\sqrt{3}}$$

$$c^2 = a^2 - b^2$$

$$c = \pm 3$$

$$2h =$$

$$a=1 \quad b=-1$$

$$\frac{2\sqrt{k^2 - ab}}{a+b}$$

$$\tan \alpha = \infty$$

$$\frac{x}{2} + \frac{y}{-4} = 1$$

Q

$$-4x + 2y = -8$$

$$4x - 2y = 8$$

$$4x - 2y - 8 = 0$$

$$2x - y - 4 = 0$$

$$\frac{\sqrt{1}}{\sqrt{2}} \cdot \frac{k}{3} = -1$$

$$k = \frac{-3\sqrt{2}}{\sqrt{1}}$$

$$\sqrt{1}x + \sqrt{2}y + \sqrt{7} = 0$$

$$\frac{\sqrt{1}}{\sqrt{2}} \cdot \frac{k}{3} = -1$$

$$k = \frac{-1 \times 3\sqrt{2}}{\sqrt{1}}$$

$$\frac{\sin^2 \alpha + \cos^2 \alpha}{\sqrt{1+t^2}} = 3 \quad \begin{matrix} t^2 + 1 = 9 \\ t^2 = 8 \end{matrix}$$

$$-4x + 2y = -8$$

$$4x - 2y = 8$$

$$2x - y = 4$$

$$\frac{\sqrt{3}}{3}i - \frac{\sqrt{3}}{3}j + \frac{\sqrt{3}}{3}k$$

$$\frac{1}{\sqrt{3}}i - \frac{1}{\sqrt{3}}j + \frac{1}{\sqrt{3}}k$$

$$\cos \alpha = \frac{1}{2}$$

$$\cos \beta = \frac{y}{|r|} = \frac{1}{\sqrt{4}} = \frac{1}{2}$$

$$\sqrt{\sin^2 \alpha + \cos^2 \alpha + t^2} = 3$$

$$\sqrt{1+t^2} = 3$$

$$t^2 + 1 = 9$$

$$t^2 = 8$$

$$\begin{vmatrix} 3 & -1 & -2 \\ 5 & 2 & -3 \\ 2 & 1 & -2 \end{vmatrix} = 0$$

$$y-6 = \frac{10}{7}(x-4)$$

$$7y - 42 = 10x - 40$$

$$10x - 7y + 2 = 0$$

$$3|-2$$

$$3(-2\alpha + 3) + 1(-10 + 6) - 2(5 - 2\alpha) = 0$$

$$-6\alpha + 9 - 4 - 10 + 4\alpha = 0$$

$$-2\alpha = 5$$

$$\begin{aligned} &(\sin(-\pi))^2 \\ &- \pi \end{aligned}$$

$$3(-2\alpha + 3)$$

$$-6\alpha + 9 + 1(-10 + 6) \neq 2(5 - 2\alpha)$$

$$-4 + 9 - 10 + 4\alpha$$

$$-5 - 2\alpha = 0$$

$$\alpha = -2.5$$

$$\frac{6+4}{4+3}$$

$$\frac{10}{7}$$

$$\frac{-3+4}{4+3} = \frac{1}{7}$$

$$\frac{-3+4}{4+3} = \frac{1}{7}$$

$$x \cos \theta + y \sin \theta = 8$$

$$\frac{\sqrt{3}x}{2} + \frac{y}{2} = 8$$

$$y = -\frac{\sqrt{3}x}{2} + 8 \times 2$$

$$y = -\sqrt{3}x + 16$$

$$y+4 = \frac{1}{7}(x+3)$$

$$7y+28 = x+3$$

$$x - 7y - 25 = 0$$

$$\sqrt{3n+5}$$

$$\sqrt{(n^2+5)-5} =$$

$$\sqrt{9n^2-8+8}$$

$$\sqrt{9n^2}$$

$$\sqrt{9n^2}$$

$$\sqrt{9n^2+5-5}$$

$$\sqrt{(n^2-5)+5}$$

$$y = 3 + \sqrt{n-2}$$

$$2n+2=0$$

$$n=-1$$

$$2 > 0$$

$$f(x) = \sin x$$

$$f'(x) = \cos x$$

$$\frac{1}{2} \frac{1}{u^2+1} \cdot 2x$$

$$\frac{1}{2} \frac{2u}{u^2+1}$$

$$\int \frac{2u}{u^2+1}$$

$$\frac{1}{2} \ln|u^2+1|$$

$$\frac{1}{2} \frac{1}{x^2+1} \cdot 2x$$

$$\frac{1}{2} \frac{2x}{x^2+1}$$

$$2 \left| \frac{u^2}{2} \right|_0^2 - 2k \left| u \right|_0^2$$

$$(2^2 - 0) - 2k(2-0)$$

$$4 - 4k = 1$$

$$4k = 3$$

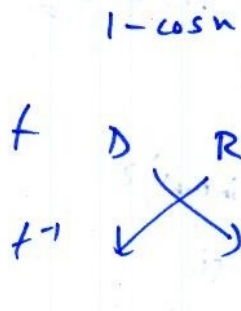
$$k = \frac{3}{4}$$

$$1 + \frac{dy}{dn} = \cos(n+y) \left[1 + \frac{dy}{dn} \right]$$

$$\frac{dy}{dn} + 1 = \cos(n+y) + \frac{dy}{dn} (\cos(n+y))$$

$$\frac{1 - \cos(n+y)}{2 \sin^2 \frac{n+y}{2}} = \frac{6+4}{4+3}$$

$$\frac{1 - \cos n}{2 \sin^2 \frac{n}{2} \cos^2 \frac{n}{2}} = \frac{10}{7}$$



$$x^2 + 4hx$$

$$f(x) = \sin x$$

$$f(x) = \sin x$$

$$f'(x) = \cos x$$

$$f'(\pi/2) = \cos 90^\circ = 0$$

$$e^{\sin x}$$

$$e^{\sin \pi/2} - e^{\sin 0}$$

$$e^1 - e^0$$

$$e - 1$$

$$2 \left| \frac{u^2}{2} \right|_0^2 - 2k(2-0) = 1$$

$$(4-0) - 4k = 1$$

$$3 = 4k$$

$$k = 3/4$$

$$u(x^2-9)$$

$$u=0 \quad x=\pm 3$$