

Q. No. 2 Part (i) (Page 1)

Euler's Theorem:-

(a) $f(x, y) = 3x^3 + 7x^2y + xy^2 + 5y^3$

$$f(x\lambda, y\lambda) = 3(x\lambda)^3 + 7(x\lambda)^2(y\lambda) + (x\lambda)(y\lambda)^2 + 5(y\lambda)^3$$

$$= 3x^3(\lambda^3) + 7x^2y(\lambda^3) + xy^2(\lambda^3) + 5y^3\lambda^3$$

$$= \lambda^3 (3x^3 + 7x^2y + xy^2 + 5y^3)$$

hence power of λ is degree of $f(x, y)$, i.e. **degree = 3**

(b)
$$x \frac{\partial}{\partial x} f(x, y) + y \frac{\partial}{\partial y} f(x, y) = n f(x, y)$$

$$\Rightarrow x \frac{\partial}{\partial x} f(x, y) = x \left\{ \frac{\partial}{\partial x} (3x^3 + 7x^2y + xy^2 + 5y^3) \right\}$$

$$= x \{ 3(3x^2) + 7y(2x) + y^2(1) + 0 \}$$

$$= x \{ 9x^2 + 14xy + y^2 \}$$

$$= 9x^3 + 14x^2y + xy^2 \quad - (1)$$

$$\Rightarrow y \frac{\partial}{\partial y} f(x, y) = y \left\{ \frac{\partial}{\partial y} (3x^3 + 7x^2y + xy^2 + 5y^3) \right\}$$

$$= y \{ 0 + 7x^2(1) + x(2y) + 5(3y^2) \}$$

$$= y \{ 7x^2 + 2xy + 15y^2 \}$$

$$= 7x^2y + 2xy^2 + 15y^3 \quad - (2)$$

\Rightarrow adding - (1) and - (2)

$$\text{L.H.S} = 9x^3 + 14x^2y + xy^2 + 7x^2y + 2xy^2 + 15y^3$$

$$= 9x^3 + 15y^3 + 3xy^2 + 21x^2y$$

$$\text{R.H.S} = 3(3x^3 + 7x^2y + xy^2 + 5y^3)$$

$$= 9x^3 + 21x^2y + 3xy^2 + 15y^3$$

$$= 9x^3 + 15y^3 + 3xy^2 + 21x^2y$$

as L.H.S = R.H.S,

$$x \frac{\partial}{\partial x} f(x, y) + y \frac{\partial}{\partial y} f(x, y) = n f(x, y) \text{ proved.}$$

Q. No. 2 Part (ii) (Page 1) Continuity :-

→ as function is continuous at $x=1$,

$$f(x) = \lim_{x \rightarrow 1} f(x) = \lim_{x \rightarrow 1} f(x)$$

$$f(x) = R \cdot H \cdot L = L \cdot H \cdot L$$

→ evaluating $f(x)$ at $x=1$

$$f(x) = 2(k-1)x$$

$$f(1) = 2(k-1)(1)$$

$$f(1) = 2k-2 \quad \text{--- (1)}$$

→ evaluating limit.

$$\lim_{x \rightarrow 1} f(x) = \lim_{x \rightarrow 1} \frac{3x^2-3}{x-1}$$

$$= \lim_{x \rightarrow 1} \frac{3(x^2-1)}{x-1}$$

$$= \lim_{x \rightarrow 1} \frac{3(x+1)(x-1)}{(x-1)}$$

$$= \lim_{x \rightarrow 1} 3(x+1)$$

$$= 3(1+1)$$

$$\lim_{x \rightarrow 1} f(x) = 6 \quad \text{--- (2)}$$

→ equating (1) and (2) as per condition of continuity.

$$6 = 2k - 2$$

$$6 + 2 = 2k$$

$$8 = 2k$$

$$4 = k$$

Thus the function is continuous at $x=1$, if

$$\boxed{k=4}$$

Q. No. 2 Part (iii) (Page 1) Newton Raphson :-

$$f(x) = x^3 - 5x + 1$$

$$f'(x) = 3x^2 - 5$$

1st iteration:

$$x_0 = 0.5$$
$$x_{0+1} = x_0 - \frac{f(x_0)}{f'(x_0)}$$

$$x_1 = 0.5 - \frac{(0.5)^3 - 5(0.5) + 1}{3(0.5)^2 - 5}$$

$$x_1 = 0.1071$$

2nd iteration:

$$x_{1+1} = x_1 - \frac{f(x_1)}{f'(x_1)}$$

$$= 0.1071 - \frac{(0.1071)^3 - 5(0.1071) + 1}{3(0.1071)^2 - 5}$$

$$= 0.20089$$

$$\approx 0.2009$$

$$\boxed{x_2 = 0.2009}$$

$$f(x_2) = 3.6 \times 10^{-3}$$

By second iteration the root = 0.2009.

(Section B)

Q. No. 2 Part (iv) (Page 1) Position Vector:-

(a) velocity vector:-

$$\vec{r}(t) = t^3 \hat{i} + e^{-2t} \hat{j} + \sin 2t \hat{k} \quad \text{diff. b.s wrt } t.$$

$$\frac{d\vec{r}(t)}{dt} = \frac{d}{dt} (t^3 \hat{i} + e^{-2t} \hat{j} + \sin 2t \hat{k})$$

$$= \frac{d}{dt} (t^3) \hat{i} + \frac{d}{dt} (e^{-2t}) \hat{j} + \frac{d(\sin 2t)}{dt} \hat{k}$$

$$\vec{v}(t) = 3t^2 \hat{i} - 2e^{-2t} \hat{j} + 2 \cos 2t \hat{k}$$

(b) acceleration vector:-

$$\frac{d\vec{v}(t)}{dt} = 3t \hat{i} \quad \text{diff again b.s wrt } t$$

$$= \frac{d(3t^2) \hat{i}}{dt} - \frac{d(2e^{-2t}) \hat{j}}{dt} + \frac{d(2 \cos 2t) \hat{k}}{dt}$$

$$= 6t \hat{i} - 2(e^{-2t})(-2) \hat{j} + 2(-\sin 2t)(2) \hat{k}$$

$$= 6t \hat{i} + 4e^{-2t} \hat{j} - 4 \sin 2t \hat{k}$$

$$= 6t \hat{i} + 4e^{-2t} \hat{j} - 4 \sin 2t \hat{k}$$

Q. No. 2 Part (iv) (Page 2)

Blank lined paper for writing the answer to Q. No. 2 Part (iv).

Q. No. 2 Part (ix) (Page 1) FIRST PRINCIPLE:-

$$y = (2x+3)^{3/2}$$

$$y + \delta y = (2(x+\delta x) + 3)^{3/2}$$

$$y + \delta y = (2x + 2\delta x + 3)^{3/2}$$

$$y + \delta y = (2x+3)^{3/2} \left\{ 1 + \frac{2\delta x}{2x+3} \right\}^{3/2}$$

$$y + \delta y = (2x+3)^{3/2} \left\{ \left(1 + \left(\frac{2\delta x}{2x+3} \right) \right)^{3/2} \right\}$$

$$\delta y = (2x+3)^{3/2} \left\{ \left(1 + \frac{2\delta x}{2x+3} \right)^{3/2} \right\} - (2x+3)^{3/2}$$

$$\delta y = (2x+3)^{3/2} \left\{ \left(1 + \left(\frac{2\delta x}{2x+3} \right) + \frac{(3/2)(3/2-1)}{2!} \left(\frac{2\delta x}{2x+3} \right)^2 + \dots \right) \right\}$$

$$\delta y = (2x+3)^{3/2} \left\{ 1 + \frac{3\delta x}{2x+3} + \frac{3}{8} \left(\frac{4\delta^2 x}{(2x+3)^2} \right) + \dots - 1 \right\}$$

$$\delta y = (2x+3)^{3/2} \left\{ \frac{3\delta x}{(2x+3)} + \frac{3}{2} \left(\frac{\delta^2 x}{(2x+3)^2} \right) + \dots \right\}$$

$$\frac{\delta y}{\delta x} = \frac{(2x+3)^{3/2}}{\delta x} \left\{ \frac{3\delta x}{(2x+3)} + \frac{3}{2} \left(\frac{\delta^2 x}{(2x+3)^2} \right) + \dots \right\}$$

$$\frac{\delta y}{\delta x} = (2x+3)^{3/2} \left\{ \frac{3}{(2x+3)} + \frac{3}{2} \left(\frac{\delta x}{(2x+3)^2} \right) + \dots \right\}$$

applying limits

$$\lim_{\delta x \rightarrow 0} \frac{\delta y}{\delta x} = \lim_{\delta x \rightarrow 0} (2x+3)^{3/2} \left\{ \frac{3}{(2x+3)} + \frac{3}{2} \left(\frac{\delta x}{(2x+3)^2} \right) \right\}$$

$$= (2x+3)^{3/2} \left\{ \frac{3}{(2x+3)} + \frac{3 \times 0}{2(2x+3)^2} \right\}$$

$$= (2x+3)^{3/2} \frac{3}{(2x+3)}$$

$$= (2x+3)^{1/2} (3)$$

$$= 3\sqrt{2x+3}$$

Q. No. 2 Part (v) (Page 1) Integration :-

$$= \int (3t+1)(t-1) dt$$

$$= \int (3t^2 - 3t + t - 1) dt$$

$$= \int (3t^2 - 2t - 1) dt$$

$$= \int 3t^2 dt - \int 2t dt - \int 1 dt$$

$$= 3 \int t^2 dt - 2 \int t dt - \int 1 dt$$

$$= \frac{3t^3}{3} - \frac{2t^2}{2} - t + C$$

$$= t^3 - t^2 - t + C$$

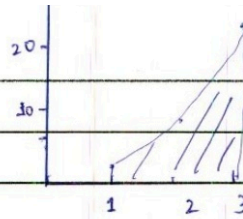
$$= t^3 - t^2 - t + C$$

Q. No. 2 Part (vi) (Page 1)

AREA:-

$$= 3x^2 - 2x$$

$$\text{area} = \int_1^3 3x^2 - 2x \, dx$$



| | | | | |
|---|---|---|---|----|
| y | 1 | 1 | 8 | 21 |
| x | 1 | 2 | 3 | |

$$= \int_1^3 3x^2 \, dx - \int_1^3 2x \, dx$$

$$= \frac{3(x^3)}{3} \Big|_1^3 - 2 \left(\frac{x^2}{2} \right) \Big|_1^3$$

$$= (x^3 - x^2) \Big|_1^3$$

$$= (3^3 - 3^2) - (1^3 - 1^2)$$

$$= 18 - (0)$$

$$= 18 \text{ units.}$$

$$= \mathbf{18 \text{ units}}$$

Q. No. 2 Part (vii) (Page 1)

Straight Lines:-

(a)

$$= 3x^2 - 2xy - 8y^2$$

$$\begin{array}{l} -2A = 6x-1 \\ -2 = -6+4 \end{array}$$

$$= 3x^2 - 6xy + 4xy - 8y^2$$

$$= 3x(x-2y) + 4y(x-2y)$$

$$= (3x+4y)(x-2y)$$

The straight lines are ① $3x+4y=0$

② $x-2y=0$

(b) $m_1 = \frac{-a}{b} = \frac{-3}{4}$

$$m_2 = \frac{-a}{b} = \frac{-1}{-2} = \frac{1}{2}$$

$$-\tan\theta = \frac{m_2 - m_1}{1 + m_1 m_2}$$

$$= \frac{(1/2) - (-3/4)}{1 + (1/2)(-3/4)}$$

$$= \frac{1 + (1/2)(-3/4)}{1 + (1/2)(-3/4)}$$

$$\tan\theta = 2$$

$$\theta = 63.43494$$

$$\theta = 63.43494^\circ$$

Q. No. 2 Part (viii) (Page 1)

Area :-

A(5,4)

B(2,1)

C(7,3)

$$\text{Area} = \frac{1}{2} \begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix}$$

$$= \frac{1}{2} \begin{vmatrix} 5 & 4 & 1 \\ 2 & 1 & 1 \\ 7 & 3 & 1 \end{vmatrix}$$

$$= \frac{1}{2} \{ 5(1-3) - 4(2-7) + 1(6-7) \}$$

$$= \frac{1}{2} (9)$$

$$= \frac{9}{2} \text{ units} = 4.5 \text{ units.}$$

Q. No. 2 Part (x) (Page 1)

Integration :-

$$\int \frac{e^x dx}{e^{2x} + 1}$$

$$\text{let } e^x = \tan \theta$$

$$e^x dx = \sec^2 \theta d\theta$$

$$\text{let } u = e^{2x} + 1$$

$$u = e^{2x} + 1$$

$$du = 2e^{2x} dx$$

$$\frac{du}{2} = e^{2x} dx$$

$$\text{hence, } = \int \frac{\tan \theta \sec^2 \theta d\theta}{(\tan^2 \theta) + 1}$$

$$= \int \frac{\sec^2 \theta d\theta}{\sec^2 \theta}$$

$$= \int d\theta$$

$$= \theta$$

$$\boxed{\tan^{-1} e^x + C}$$

$$\text{as } e^x = \tan \theta$$

$$\tan^{-1} e^x = \theta$$

$$= \tan^{-1} e^x + C$$

Q. No. 2 Part (xi) (Page 1) Partial Differentiation:-

$$f(x, y) = \sqrt{x^3 + y^3}$$

$$(a) \frac{\partial f}{\partial x} = \frac{\partial}{\partial x} \sqrt{x^3 + y^3}$$

$$= \frac{1}{2\sqrt{x^3 + y^3}} \left(\frac{\partial}{\partial x} x^3 + \frac{\partial}{\partial x} y^3 \right)$$

$$= \frac{1}{2\sqrt{x^3 + y^3}} (3x^2 + 0)$$

$$= \frac{3x^2}{2\sqrt{x^3 + y^3}}$$

$$= \frac{3x^2}{2\sqrt{x^3 + y^3}}$$

$$(b) \frac{\partial f}{\partial y} = \frac{\partial}{\partial y} \sqrt{x^3 + y^3}$$

$$= \frac{1}{2\sqrt{x^3 + y^3}} \left(\frac{\partial}{\partial y} x^3 + \frac{\partial}{\partial y} y^3 \right)$$

$$= \frac{1}{2\sqrt{x^3 + y^3}} (0 + 3y^2)$$

$$= \frac{3y^2}{2\sqrt{x^3 + y^3}}$$

Q. No. 2 Part (xii) (Page 1) $\frac{dy}{dx}$ calculation:-

$$x^3 + 3x^2y^2 + y^3 = 0$$

$$\frac{d}{dx} (x^3 + 3x^2y^2 + y^3) = \frac{d}{dx} (0)$$

$$\frac{d}{dx} (x^3) + \frac{d}{dx} (3x^2y^2) + \frac{d}{dx} (y^3) = 0$$

$$3x^2 + 3 \left\{ x^2 (2y) \frac{dy}{dx} + y^2 (2x) \right\} + 3y^2 \frac{dy}{dx} = 0$$

$$3x^2 + 6x^2y \frac{dy}{dx} + 6xy^2 + 3y^2 \frac{dy}{dx} = 0$$

$$3x^2 + 6xy^2 = \frac{dy}{dx} (-6x^2y - 3y^2)$$

$$\frac{3x^2 + 6xy^2}{-6x^2y - 3y^2} = \frac{dy}{dx}$$

$$\frac{x^2 + 2xy^2}{-2x^2y - y^2} = \frac{dy}{dx}$$

Q. No. 3 (Page 1)

Equations:-

$$(a) \frac{x^3}{8} + \frac{x^2}{4} + \frac{2}{x^2} + \frac{1}{2}$$

(a) tangent equation at $x=2$

$$y = \frac{x^3}{8} + \frac{x^2}{4} + \frac{2}{x^2} + \frac{1}{2}$$

$$\frac{dy}{dx} = \frac{1}{8}(3x^2) + \frac{1}{4}(2x) + 0 + 2(-2)x^{-2-1}$$

$$\frac{dy}{dx} = \frac{3x^2}{8} + \frac{x}{2} - \frac{4}{x^3}$$

put $x=2$ for m .

$$m = \frac{3(2)^2}{8} + \frac{2}{2} - \frac{4}{(2)^3}$$

$$m = 2$$

if $x=2$, $y = \frac{2^3}{8} + \frac{2^2}{4} + \frac{2}{2^2} + \frac{1}{2}$

$$y = 3$$

equation of tangents

~~$y=mx$~~

~~$$(y-2) = 2(x-3)$$~~

$$(y-3) = 2(x-2)$$

~~$$y-2 = 2x-6$$~~

$$y-3 = 2x-4$$

~~$$y-2x = 2-6$$~~

$$y-2x = 3-4$$

~~$$y-2x = -4$$~~

$$y-2x = -1$$

~~$$y-2x+4=0$$~~

$$y-2x+1=0$$

~~$$-2x+y+4=0$$~~

$$2x-y-1=0$$

~~$$2x-y-4=0$$~~

(b) equation of normal:

$$(y-3) = -\frac{1}{m}(x-2)$$

$$(y-3) = -\frac{1}{2}(x-2)$$

$$2y-6 = -x+2$$

$$2y+x = 6+2$$

$$2y+x = 8$$

$$x+2y-8=0$$

$$x+2y-8=0$$

(c) continuity :-

for a function to be continuous at $x=0$,① $f(0)$ must be defined

② limit must exist

③ $R.H.L = L.H.L = f(c)$ thus checking continuity at $x=0$.

$$= \frac{x^3}{8} + \frac{x^2}{4} + \frac{2}{x^2} + \frac{1}{2}$$

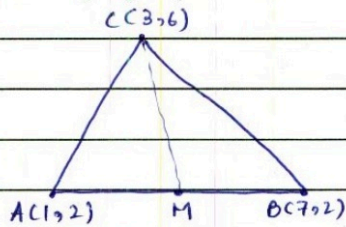
$$= \frac{0}{8} + \frac{0}{4} + \frac{2}{0} + \frac{1}{2}$$

$$= 0 + 0 + \frac{1}{0} + \infty$$

as function is undefined at $x=0$,
function is discontinuous at $x=0$.

Q. No. 4 (Page 1)

ΔABC :-



(a) Median \overline{CM}

$$M = \left(\frac{1+7}{2}, \frac{2+2}{2} \right)$$

$$= (4, 2)$$

Now finding median,

$$(x_1, y_1) = (3, 6)$$

$$\frac{(y - y_1)}{(y_2 - y_1)} = \frac{(x - x_1)}{(x_2 - x_1)}$$

$$(x_2, y_2) = (4, 2)$$

$$\frac{(y - 6)}{(2 - 6)} = \frac{(x - 3)}{(4 - 3)}$$

$$\frac{(y - 6)}{2 - 6} = \frac{(x - 3)}{4 - 3}$$

$$\frac{(y - 6)}{-4} = \frac{(x - 3)}{1}$$

$$(y - 6) = -4(x - 3)$$

$$y - 6 = -4x + 12$$

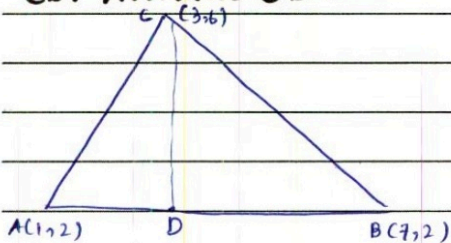
$$y + 4x = 12 + 6$$

$$y + 4x = 18$$

$$y + 4x = 18$$

$$4x + y - 18 = 0$$

(b) Altitude \overline{CD} :-



$$(x_1, y_1) = (3, 6)$$

$$\text{slope of AB} = \frac{2-2}{7-1} = 0$$

$$\text{slope of CD} = -\frac{1}{\text{slope of AB}}$$

$$= -\frac{1}{0}$$

$$(y - y_1) = m(x - x_1)$$

$$y - 6 = -\frac{1}{0}(x - 3)$$

$$(y - 6)(0) = -(x - 3)$$

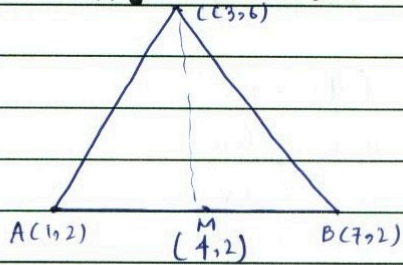
$$(y - 6)(0) = 3 - x$$

$$0 = 3 - x$$

$$x - 3 = 0$$

Q. No. 4 (Page 2)

(c) Right bisector :-



$$(x_1, y_1) = (4, 2)$$

$$\text{slope of } \overline{AB} = \frac{2-2}{7-1} = 0$$

$$\text{slope of } \overline{CM} = \frac{-1}{0}$$

$$(y - y_1) = (m)(x - x_1)$$

$$(y - 2) = \frac{-1}{0} (x - 4)$$

$$0(y - 2) = -x + 4 \quad 0 = -(x - 4)$$

$$y + x = 2 + 4 \quad 0 = -x + 4$$

$$y + x = 6 \quad 0 = -x + 4$$

$$x - 4 = 0$$

$$\mathbf{x - 4 = 0}$$

Q. No. 5 (Page 1)

$$\int \frac{2x-1}{x^3-x^2-2x} dx$$

$$= x^3 - x^2 - 2x$$

$$= x^3 - 2x^2 + x^2 - 2x$$

$$= \int \frac{2x-1}{x(x+1)(x-2)} dx$$

$$= x^2(x-2) + x(x-2)$$

$$= (x^2+x)(x+2)$$

by partial fractions,

$$= x(x+1)(x-2)$$

$$\frac{2x-1}{x(x+1)(x-2)} = \frac{A}{x} + \frac{B}{x+1} + \frac{C}{x-2}$$

$$2x-1 = A(x+1)(x-2) + B(x)(x-2) + C(x)(x+1)$$

$$2x-1 = A(x^2-2x+x-2) + B(x^2-2x) + C(x^2+x)$$

$$2x-1 = Ax^2 - 2Ax + Ax - 2A + Bx^2 - 2Bx + Cx^2 + Cx$$

$$2x-1 = x^2(A+B+C) + x(-2A-2B+C) - 2A$$

put $x=2$

$$2(2)-1 = A(2+1)(2-2) + B(2)(2-2) + C(2)(2+1)$$

$$4-1 = C(6)$$

$$\frac{3}{6} = C$$

put $x=-1$

$$2(-1)-1 = A(-1+1)(-1-2) + B(-1)(-1-2) + C(-1)(-1+1)$$

$$-3 = B(3)$$

$$-1 = B$$

put $x=0$

$$2(0)-1 = A(0+1)(0-2) + B(0) + C(0)$$

$$-1 = -2A$$

$$1/2 = A$$

$$C = 1/2, A = 1/2, B = -1$$

Q. No. 5 (Page 2)

$$\int \frac{2x-1}{x^3-x^2-2x} dx = \int \frac{A dx}{x} + \int \frac{B dx}{x+1} + \int \frac{C dx}{x-2}$$

$$= \int \frac{1/2}{x} dx + \int \frac{-1}{x+1} dx + \int \frac{1/2}{x-2} dx$$

$$= \frac{1}{2} \int \frac{dx}{x} - \int \frac{dx}{x+1} + \frac{1}{2} \int \frac{dx}{x-2}$$

$$= \frac{1}{2} \ln x - \ln(x+1) + \frac{1}{2} \ln(x-2) + C$$

$$= \frac{1}{2} \ln x - \ln(x+1) + \frac{1}{2} \ln(x-2) + C$$

$$= \frac{1}{2} \ln x - \ln(x+1) + \frac{1}{2} \ln(x-2) + C$$

Q. No. 6 (Page 1)

SIMPSON'S RULE:-

$$\int_0^2 (3x^2 - 2x) dx$$

$$h = \frac{b-a}{2n} = \frac{2-0}{2(2)} = \frac{2}{4} = \frac{1}{2}$$

$$\frac{h}{3} \{ f(x_0) + f(x_4) + 4(f(x_1) + f(x_3)) + 2(f(x_2)) \}$$

| | | | | | |
|------|-------------------|-------------------|-------------------|-------------------|-------------------|
| f(x) | 0 | -1/4 | 1 | 3.75 | 8 |
| (x) | 0 | 1/2 | 1 | 3/2 | 2 |
| | (x ₀) | (x ₁) | (x ₂) | (x ₃) | (x ₄) |

$$= \frac{1/2}{3} \{ 0 + 8 + 4(-0.25 + 3.75) + 2(1) \}$$

$$= \frac{1}{6} \{ 8 + \frac{3+15}{2} \}$$

$$= \frac{12}{6}$$

$$= 2$$

$$= \frac{1}{6} \{ 0 + 8 + 4(-0.25 + 3.75) + 2(1) \}$$

$$= \frac{1}{6} \{ 8 + 14 + 2 \}$$

$$= \frac{24}{6}$$

$$= 4$$

(a) $\int_0^2 (3x^2 - 2x) dx$ by Simpson's = 4

(b) Actual integral:-

$$= \int_0^2 (3x^2 - 2x) dx$$

$$= \frac{3x^3}{3} - \frac{2x^2}{2} \Big|_0^2$$

$$= (x^3 - x^2) \Big|_0^2$$

$$= (2^3 - 2^2) - (0^3 - 0^2)$$

$$= 4 \text{ units}$$

Q. No. 6 (Page 2)

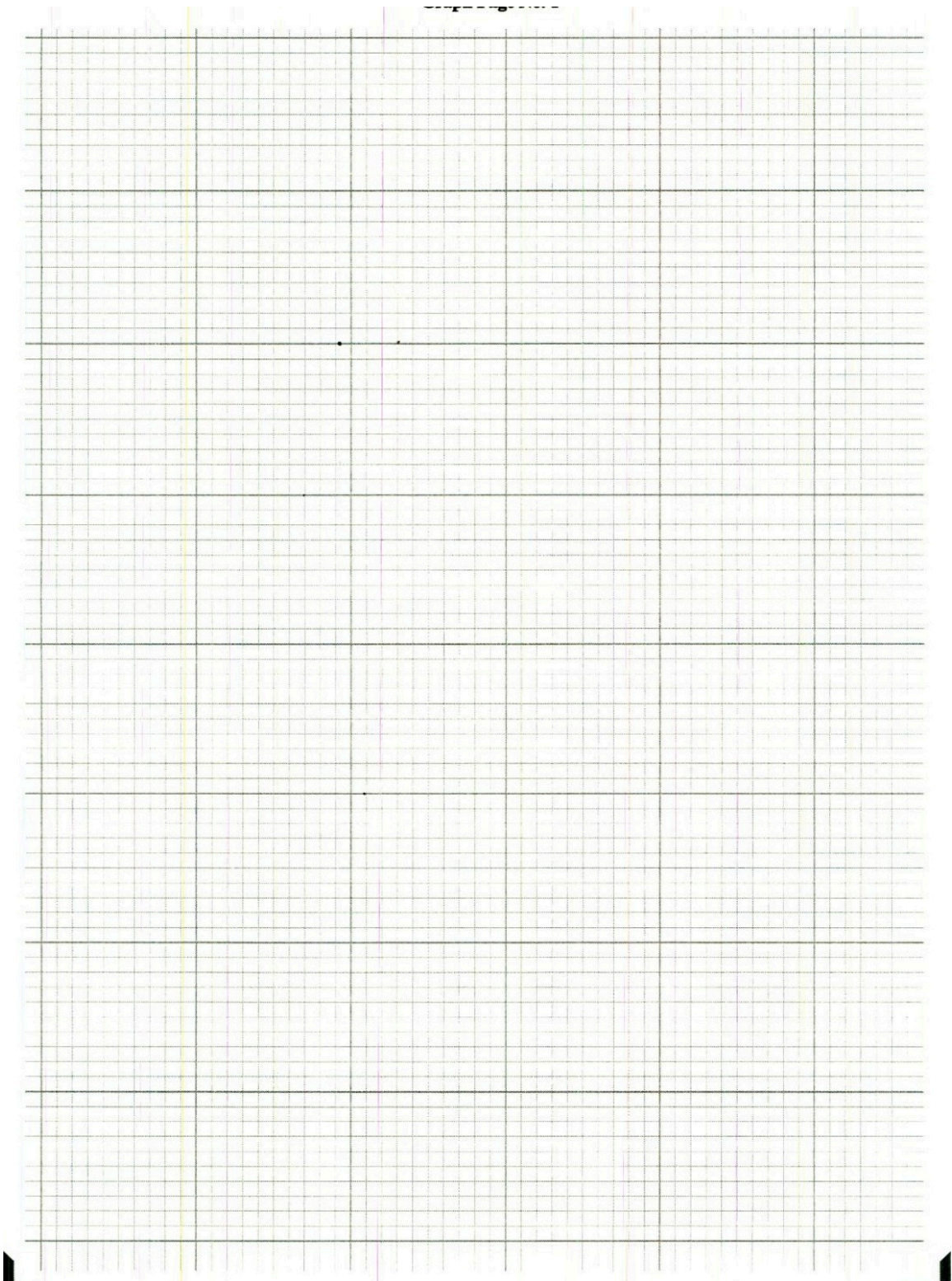
(c) Difference:-

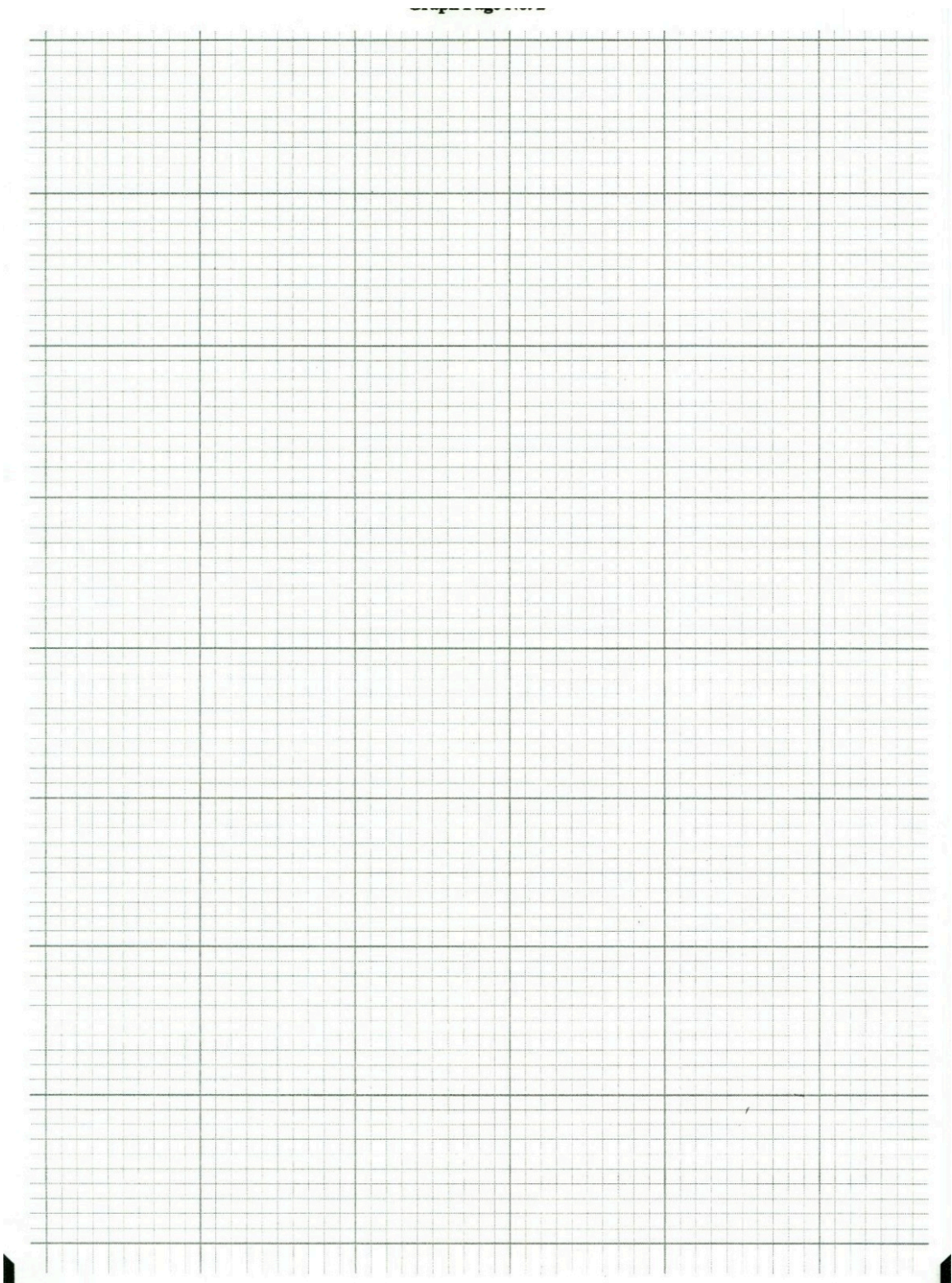
$$= \text{Actual value} - \text{estimated value}$$

$$= 4 - 4$$

$$= 0.$$

which means 100% accurate results.





$$= x^3 - 2x^2 + x^2 - 2x \quad yz(2x+3)^{3/2}$$

$$= x^2(x-2) + x(x-2)$$

$$= (x^2+x)(x-2)$$

$$= x(x+1)(x-2)$$

$$y+8y = (2x+28x+3)^{3/2} - (2x+3)^{3/2}$$

$$= (2x+3)^{3/2} \left\{ 1 + \frac{28x}{2x+3} \right\}^{3/2} - (2x+3)^{3/2}$$

$$\frac{2x-1}{x} = \frac{A}{x} + \frac{B}{x+1} + \frac{C}{x-2}$$

$$(2x-1) = A(x+1)(x-2) + B(x)(x-2) + C(x)(x+1)$$

$$= (2x+3)^{3/2} \left\{ 1 + \frac{3}{2} \left(\frac{28x}{2x+3} \right) \right\}$$

put $x = -1$

$$-3 = B(-1)(-1-2)$$

$$-3 = 3B$$

$$-1 = B$$

put $x = 2$

$$2(2)-1 = (2)(2+1)$$

$$C = 1/2$$

put $x = 0$

$$2(0)-1 = A(0+1)(0-2)$$

$$-1 = A(-2)$$

$$1/2 = A$$

$$\frac{1}{2} C$$

$$\frac{1}{2} x^2 - \frac{1}{2} (2/x) + \frac{x}{2} \cdot 2 \left(\frac{1}{2} \right) + 0 \left(\frac{1}{2} \right)$$

$$+ (-1)(x^2) - 2(x)(x-1)$$

$$+ \frac{1}{2} x^2 + \frac{1}{2} x$$

$$2 - \frac{x^2}{2} = 0 + 2x - 1$$

$$\frac{3}{2} (2x+3)(2)$$

$$(1 + \frac{2}{x})^2$$

$$e^x + 2(e^{-2x})(-2)$$

$$= e^x - 4e^{-2x}$$

$$a) \frac{1}{8} \{ 8 \cos 2x \cos 2x \}$$

$$= \frac{2}{8} (\cos 2x)$$

$$f''(x) = \frac{2}{8} (-\sin 2x)(2)$$

$$= \frac{1}{2} (-\sin 2x)$$

$$f'''(x) = \frac{1}{2} (-\cos 2x)(2)$$

$$= -\cos 2x$$

$$f''''(x) = -(-\sin 2x)(2)$$

$$= 2 \sin 2x$$

$$\frac{1}{x} \frac{dy}{dx} = 2$$

$$dy = 2x dx$$

$$y = \frac{2x^2}{2} + c$$

$$y = x^2 + c$$

$$\frac{2 \cdot 0}{4} = 1/2$$

$$0 \quad 0.5 \quad 1 \quad 1.5 \quad 2$$

$$1 \quad 1/4 \quad 2 \quad 1.5 \quad 5$$

$$\frac{1}{2} \div \frac{2}{1}$$

$$1 \quad 0 \quad 0.5 \quad 1 \quad 1.5 \quad 2$$

$$1 \quad 1/4 \quad 2 \quad 1.5 \quad 5$$

$$\frac{1}{4} \{ 1 + 5 + \dots \}$$

$$\frac{13}{3} + x$$

$$\begin{vmatrix} 1 & 0 & -1 \\ 1 & 0 & -3 \\ 4 & 1 & -1 \end{vmatrix}$$

$$\frac{3}{2} (\frac{1}{2})^x \ln(\frac{1}{2}) - 2$$

$$= \frac{3}{4} x^{-1/2} - 2$$

$$= \frac{3}{4}$$

$$2 \hat{i} - 2 \hat{j}$$

$$\int \frac{\cos x dx}{\sin x}$$

en (sin x) + c

$$(\frac{5 + (-2) + 0}{3}), (\frac{-5 + 0 + 2}{2})$$

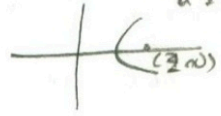
$$C(x+1)^2 + (y+1)^2 = 4 \quad (1, -1)$$

$$2yx = 4x \quad 2fy = 4y$$

$$y = 2 \quad f = 2$$

$$\sqrt{2^2 + 2^2} = c$$

$$\sqrt{4+4}$$



$$e^{x+y} (0+1)$$

$$= e^{1+0}$$

$$= e^1$$

$$2x = 2(1)$$

$$\frac{2x^2}{2}$$

$$\frac{x^2}{1-0} = 3k-2 \quad \frac{2 \cdot 0}{2} = \frac{2}{2} = 1$$

$$3x^2 - 2 \quad 6 = 2 \cdot 3$$

$$= 3(0)^2 - 2$$

$$= -2$$

$$\begin{vmatrix} 0 & 1 & 2 \\ 1 & 2 & 5 \end{vmatrix}$$

$$\frac{1}{2} \{ 1 + 5 + 2(2) \}$$

$$\frac{1}{2} \{ 6 + 4 \}$$

$$2x + 0 = 2(1)$$

$$y = x + 0 = 1$$

$$2 + (\frac{x}{x}) x = R$$

$$(x) x dx = R$$

$$dy = 2 dx$$

$$x = \frac{dy}{2}$$

$$\frac{x}{2} = R$$

$$e^{x+y} (1+0)$$

$$e^{x+y} (1)$$

$$e^{1+0}$$

