

Q. No. 2 Part (i)  $x^2 - 2x + p = 0$

let roots of equation be  $\alpha$  and  $\beta$ .

$$\alpha + \beta = \frac{-b}{a} = \frac{-(-2)}{1} = 2 \quad a=1 \quad b=-2 \quad c=p$$

$$\alpha\beta = \frac{c}{a} = \frac{p}{1} = p$$

$$\alpha + \beta = 2 \rightarrow \text{(i)}$$

$$\alpha\beta = p \rightarrow \text{(ii)}$$

$$3\alpha + 4\beta = 5 \rightarrow \text{(iii)}$$

Using eq (i) & (iii)

Multiplying eq (i) by 3 on both sides,

$$3(\alpha + \beta = 2)$$

$$3\alpha + 3\beta = 6$$

Now Subtracting the equations,

$$3\alpha + 3\beta = 6$$

$$- \quad \ominus 3\alpha \quad \oplus 4\beta = \ominus 5$$

$$-\beta = 1$$

$$\beta = -1$$

Now,

$$\alpha + \beta = 2$$

$$\alpha - 1 = 2$$

$$\alpha = 2 + 1$$

$$\alpha = 3$$

Now put values of  $\alpha$  &  $\beta$  in eq (ii)

$$\rightarrow \alpha\beta = p$$

$$(3)(-1) = p$$

$$-3 = p$$

$$p = -3$$



Q. No. 2 Part (ii)

$$\sqrt{x-3} + 5 = x$$

$$\sqrt{x-3} = -5 + x$$

Taking square on both sides,

$$(\sqrt{x-3})^2 = (-5+x)^2$$

$$x-3 = (-5)^2 + (x)^2 + 2(-5)(x)$$

$$x-3 = 25 + x^2 - 10x$$

$$x^2 - 10x - x + 25 + 3 = 0$$

$$x^2 - 11x + 28 = 0$$

$$x^2 - 7x - 4x + 28 = 0$$

$$x(x-7) - 4(x-7) = 0$$

$$(x-7)(x-4) = 0$$

$$x-7 = 0$$

$$x = 7$$

$$x-4 = 0$$

$$x = 4$$

Now Checking,

$$\sqrt{x-3} + 5 = x$$

$$\sqrt{7-3} + 5 = 7$$

$$\sqrt{4} + 5 = 7$$

$$2 + 5 = 7$$

$$7 = 7$$

It is true.

Now Checking,

$$\sqrt{x-3} + 5 = x$$

$$\sqrt{4-3} + 5 = 4$$

$$\sqrt{1} + 5 = 4$$

$$1 + 5 = 4$$

$$6 \neq 4$$

It is not true.

(extraneous root)

$$S.S = \{7\}$$



Q. No. 2 Part (iii)

$$\frac{x}{p} = \frac{y}{q} = \frac{z}{r} \text{ then } \frac{x^3 + y^3 + z^3}{p^3 + q^3 + r^3} = \frac{xyz}{pqr}$$

By k-method,

$$\frac{x}{p} = \frac{y}{q} = \frac{z}{r} = k$$

$$x = pk, \quad y = qk, \quad z = rk$$

$$\text{L.H.S} = \frac{x^3 + y^3 + z^3}{p^3 + q^3 + r^3}$$

$$= \frac{(pk)^3 + (qk)^3 + (rk)^3}{p^3 + q^3 + r^3}$$

$$= \frac{p^3 k^3 + q^3 k^3 + r^3 k^3}{p^3 + q^3 + r^3}$$

$$= \frac{k^3 (p^3 + q^3 + r^3)}{p^3 + q^3 + r^3}$$

$$= k^3 \rightarrow (i)$$

$$\text{R.H.S} = \frac{xyz}{pqr}$$

$$= \frac{(pk)(qk)(rk)}{pqr}$$

$$= k \cdot k \cdot k$$

$$= k^3 \rightarrow (ii)$$

From (i) & (ii),

$$\text{L.H.S} = \text{R.H.S}$$



Q. No. 2 Part (iv)

$$A = \{1, 2, 3, 4\}$$

$$B = \{2, 3, 5, 7\}$$

$$A \times B = \{(1, 2), (1, 3), (1, 5), (1, 7), (2, 2), (2, 3), (2, 5), (2, 7), (3, 2), (3, 3), (3, 5), (3, 7), (4, 2), (4, 3), (4, 5), (4, 7)\}$$

$$R = \{(x, y) \mid x \in A, y \in B \wedge y < x\}$$

$$R = \{(3, 2), (4, 2), (4, 3)\}$$



(i) ←

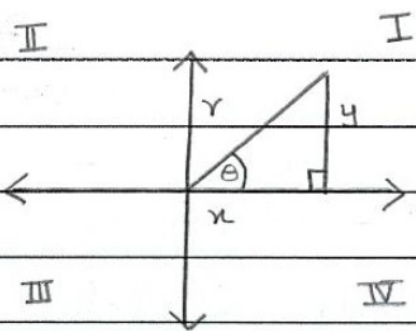
(ii) ←

(iii) & (iv)

$$Z \cdot H \cdot R = Z \cdot H \cdot J$$

Q. No. 2 Part (v)

$\theta$  lies in I quadrant.



$$\sin \theta = \frac{3}{4}$$

$$\sin \theta = \frac{P}{H} = \frac{y}{r} = \frac{3}{4}$$

$$y = 3, r = 4, x = ?$$

$$\therefore r^2 = x^2 + y^2$$

$$x^2 = r^2 - y^2$$

$$x = \sqrt{r^2 - y^2}$$

$$x = \sqrt{(4)^2 - (3)^2}$$

$$x = \sqrt{16 - 9}$$

$$x = \sqrt{7}$$

$$x = \sqrt{7}, y = 3, r = 4$$

$$\operatorname{cosec} \theta = \frac{H}{P} = \frac{r}{y} = \frac{4}{3} \rightarrow$$

$$\operatorname{cosec} \theta = \frac{4}{3}$$

$$\cos \theta = \frac{B}{H} = \frac{x}{r} = \frac{\sqrt{7}}{4} \rightarrow$$

$$\cos \theta = \frac{\sqrt{7}}{4}$$

$$\sec \theta = \frac{H}{B} = \frac{r}{x} = \frac{4}{\sqrt{7}} \rightarrow$$

$$\sec \theta = \frac{4}{\sqrt{7}}$$

$$\tan \theta = \frac{P}{B} = \frac{y}{x} = \frac{3}{\sqrt{7}} \rightarrow$$

$$\tan \theta = \frac{3}{\sqrt{7}}$$

$$\cot \theta = \frac{B}{P} = \frac{x}{y} = \frac{\sqrt{7}}{3} \rightarrow$$

$$\cot \theta = \frac{\sqrt{7}}{3}$$



Q. No. 2 Part (vi)  $\frac{20}{(x-3)(x^2+1)}$

$$\frac{20}{(x-3)(x^2+1)} = \frac{A}{x-3} + \frac{Bx+C}{x^2+1}$$

Multiplying both sides by  $D(x) = (x-3)(x^2+1)$

$$20 = A(x^2+1) + (Bx+C)(x-3)$$

$$20 = Ax^2 + A + Bx^2 - 3Bx + Cx - 3C \rightarrow (i)$$

By Zero's method,

$$x-3 = 0 \Rightarrow \underline{x=3}, \text{ put } x=3 \text{ in eq. (i)}$$

$$20 = A(3)^2 + A + B(3)^2 - 3B(3) + C(3) - 3C$$

$$20 = 9A + A + \cancel{9B} - \cancel{9B} + \cancel{3C} - \cancel{3C}$$

$$20 = 10A$$

$$A = \frac{20}{10} \Rightarrow \boxed{A=2}$$

Now,

Comparing coefficients of  $x^2$  on both sides,

$$0 = A + B$$

$$0 = 2 + B$$

$$\boxed{B = -2}$$

Next,

Comparing coefficients of  $x$  on both sides,

$$0 = -3B + C$$

$$0 = -3(-2) + C$$

$$0 = 6 + C$$

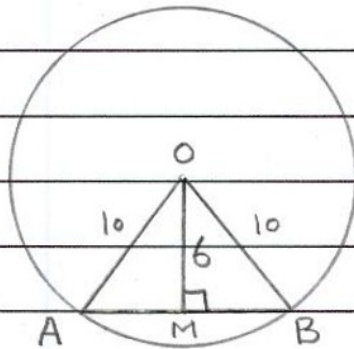
$$\boxed{C = -6}$$

$$\frac{20}{(x-3)(x^2+1)} = \frac{2}{x-3} + \frac{-2x-6}{x^2+1}$$

$$\frac{20}{(x-3)(x^2+1)} = \frac{2}{x-3} + \frac{-(2x+6)}{x^2+1}$$

$$\therefore \frac{20}{(x-3)(x^2+1)} = \frac{2}{x-3} - \frac{2x+6}{x^2+1}$$

Q. No. 2 Part (vii)



In  $\triangle OMB$ ,

$$H^2 = B^2 + P^2$$

$$(OB)^2 = (BM)^2 + (OM)^2$$

$$(10)^2 = (BM)^2 + (6)^2$$

$$(BM)^2 = (10)^2 - (6)^2$$

$$(BM)^2 = 100 - 36$$

$$(BM)^2 = 64$$

$$\sqrt{(BM)^2} = \sqrt{64}$$

$$\therefore \overline{BM} = 8 \text{ cm}$$

As,  $\overline{BM} + \overline{AM} = \overline{AB}$

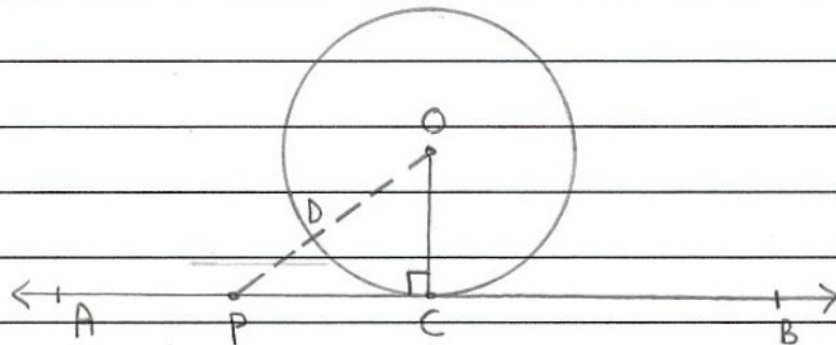
$$\overline{AB} = 2(\overline{BM}) \quad \therefore \{ \overline{AM} = \overline{BM} \Rightarrow 2\overline{BM} \}$$

$$\overline{AB} = 2(8)$$

$$\overline{AB} = 16 \text{ cm}$$

Q. No. 2 Part (viii) If a line is ..... at that point.

**THEOREM :-**



**Given :-**

A circle with O has radial segment  $\overline{OC}$ .  $\overleftrightarrow{AB}$  is a line drawn to circle such that  $\overleftrightarrow{AB} \perp \overline{OC}$  at C.

**To prove :-**  $\overleftrightarrow{AB}$  is tangent to circle at C.

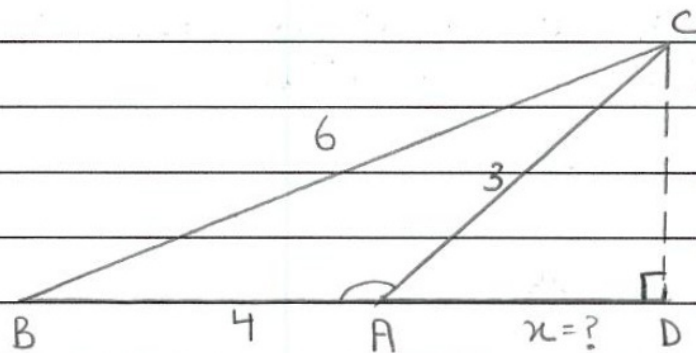
**Construction :-** Take point P on  $\overleftrightarrow{AB}$  other than C and join P to O to form  $\triangle OCP$ .

**Proof :-**

Statements	Reasons
In $\triangle OCP$ ,	
$\angle OCP = 90^\circ$	given
$\angle OPC < 90^\circ$	acute angle of right triangle
$\overline{OP} > \overline{OC}$	greater angle has greater side opposite to it.
Point P lies outside circle	$\overline{OC}$ is the radial segment
So, every point on $\overleftrightarrow{AB}$ except C lies outside the circle.	—
So $\overleftrightarrow{AB}$ touches circle at one point only.	—
Hence $\overleftrightarrow{AB}$ is tangent to the circle at point C.	



Q. No. 2 Part (ix)



By Theorem,

$$(\overline{BC})^2 = (\overline{AB})^2 + (\overline{AC})^2 + 2(\overline{AB})(\overline{AD})$$

$$\overline{BC} = 6, \quad \overline{AB} = 4, \quad \overline{AC} = 3, \quad (\overline{AD}) = ?$$

$$(6)^2 = (4)^2 + (3)^2 + 2(4)(\overline{AD})$$

$$36 = 16 + 9 + 8(\overline{AD})$$

$$36 - 16 - 9 = 8(\overline{AD})$$

$$11 = 8(\overline{AD})$$

$$\overline{AD} = \frac{11}{8}$$

$$\overline{AD} = 1.375 \text{ cm}$$

$$\boxed{x = 1.375 \text{ cm}}$$

Q. No. 3 (Page 1)

$$\frac{x + 7a}{x - 7a} + \frac{x + 7b}{x - 7b} = 2 \text{ if } x = \frac{14ab}{a+b}$$

$$x = \frac{14ab}{a+b}$$

$$x = \frac{7a \times 2b}{a+b}$$

$$\frac{x}{7a} = \frac{2b}{a+b}$$

Using componendo - dividendo theorem,

$$\frac{x + 7a}{x - 7a} = \frac{2b + (a+b)}{2b - (a+b)}$$

$$\frac{x + 7a}{x - 7a} = \frac{2b + a + b}{2b - a - b}$$

$$\frac{x + 7a}{x - 7a} = \frac{3b + a}{b - a} \rightarrow (i)$$

Now,  $x = \frac{14ab}{a+b}$

$$x = \frac{2a \times 7b}{a+b}$$

$$\frac{x}{7b} = \frac{2a}{a+b}$$

Using componendo - dividendo theorem,

$$\frac{x + 7b}{x - 7b} = \frac{2a + (a+b)}{2a - (a+b)}$$

$$\frac{x + 7b}{x - 7b} = \frac{2a + a + b}{2a - a - b}$$

Q. No. 3 (Page 2)

$$\frac{x+7b}{x-7b} = \frac{3a+b}{a-b} \rightarrow \text{(ii)}$$

Now adding eq (i) & (ii) on both sides,

$$\frac{x+7a}{x-7a} + \frac{x+7b}{x-7b} = \frac{3b+a}{b-a} + \frac{3a+b}{a-b}$$

$$= \frac{3b+a}{b-a} + \frac{3a+b}{-(b-a)}$$

$$= \frac{3b+a}{b-a} - \frac{3a+b}{b-a}$$

$$= \frac{3b+a - (3a+b)}{b-a}$$

$$= \frac{3b+a - 3a - b}{b-a}$$

$$= \frac{2b-2a}{b-a}$$

$$= \frac{2(b-a)}{b-a}$$

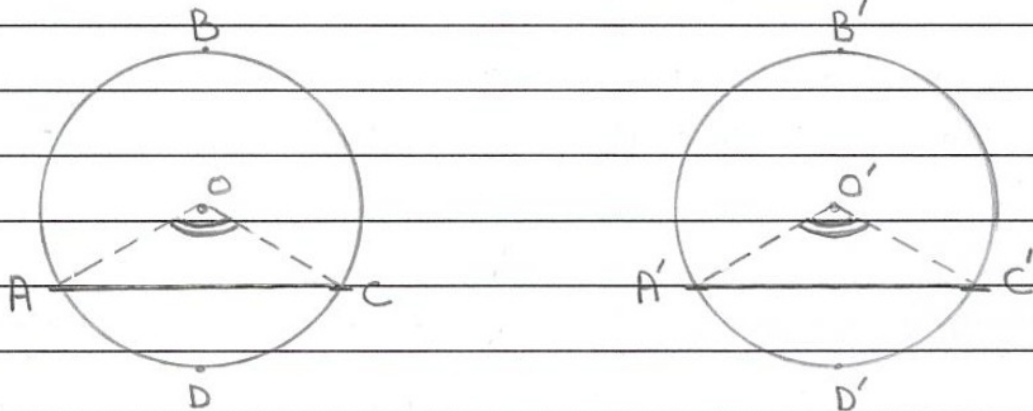
$$\therefore \frac{x+7a}{x-7a} + \frac{x+7b}{x-7b} = 2$$

Hence proved.

Q. No. 4 (Page 1)

### THEOREM :-

If two arcs of a circle (or of congruent circles) are congruent, then the corresponding chords are equal :-



Given :-

ABCD and A'B'C'D' are two <sup>congruent</sup> circles with centres O and O' respectively. Arcs  $\widehat{ADC} \cong \widehat{A'D'C'}$

To prove :-

$$\overline{AC} = \overline{A'C'}$$

Construction :-

Join O to A and C and O' to A' and C' to form  $\triangle AOC$  and  $\triangle A'O'C'$  respectively.

Proof :-

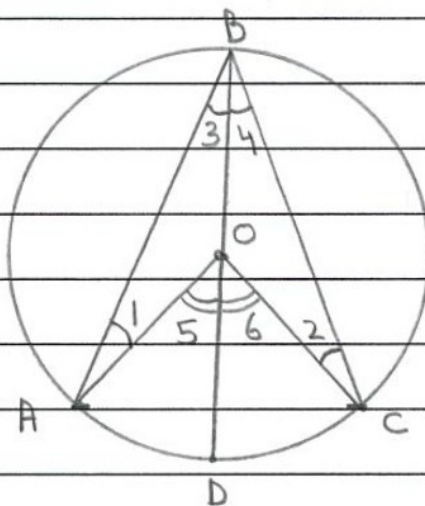
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Statements	Reasons
<p>ABCD and A'B'C'D' are two circles with centres O &amp; O'</p>	<p>given</p>
<p><math>\widehat{ADC} = \widehat{A'D'C'}</math></p>	<p>given</p>
<p><math>\therefore \angle AOC = \angle A'O'C'</math></p>	<p>central angles subtended by two equal arcs are always equal</p>
<p>Now, <math>\triangle AOC \leftrightarrow \triangle A'O'C'</math></p>	
<p><math>\overline{OA} \cong \overline{O'A'}</math></p>	<p>radii of congruent circles</p>
<p><math>\overline{OC} \cong \overline{O'C'}</math></p>	<p>radii of congruent circles</p>
<p><math>\angle AOC \cong \angle A'O'C'</math></p>	<p>already proved.</p>
<p><math>\triangle AOC \cong \triangle A'O'C'</math></p>	<p>S.A.S <math>\cong</math> S.A.S</p>
<p>Thus,</p>	
<p><math>\overline{AC} \cong \overline{A'C'}</math></p>	<p>corresponding sides</p>
	<p>of two congruent</p>
	<p>triangles.</p>

Q. No. 5 (Page 1)

### THEOREM :-

The measure of central angle of a minor arc of a circle is double that of the angle subtended by corresponding major arc.



Given :-

A circle with centre O has minor arc  $\widehat{AC}$  and major arc  $\widehat{ABC}$ .  $\angle AOC$  is central angle subtended by minor arc and  $\angle ABC$  is circum angle subtended by major arc.

To prove :-

$$\angle AOC = 2\angle ABC$$

Construction :-

Join B to O and produce it to meet the circle at D. Label angles;  $\angle 1, \angle 2, \angle 3, \angle 4, \angle 5, \angle 6$ .

**Proof :-**

Statements	Reasons
In $\triangle AOB$ ,	
$\angle 1 = \angle 3$ (i)	angles opposite to two equal sides in $\triangle AOB$ .
In $\triangle BOC$ ,	
$\angle 2 = \angle 4$ (ii)	angles opposite to two equal sides in $\triangle BOC$ .
$\angle 5 = \angle 1 + \angle 3$ (iii)	exterior angle is equal to sum of interior opposite angles
$\angle 6 = \angle 2 + \angle 4$ (iv)	as in above.
$\angle 5 = \angle 3 + \angle 3 = 2m\angle 3$ (v)	Using (i) & (iii)
$\angle 6 = \angle 4 + \angle 4 = 2m\angle 4$ (vi)	Using (ii) & (iv)
$\angle 5 + \angle 6 = 2m\angle 3 + 2m\angle 4$ $= 2(\angle 3 + \angle 4)$	adding (v) & (vi)
$\angle AOC = 2\angle ABC$	

100

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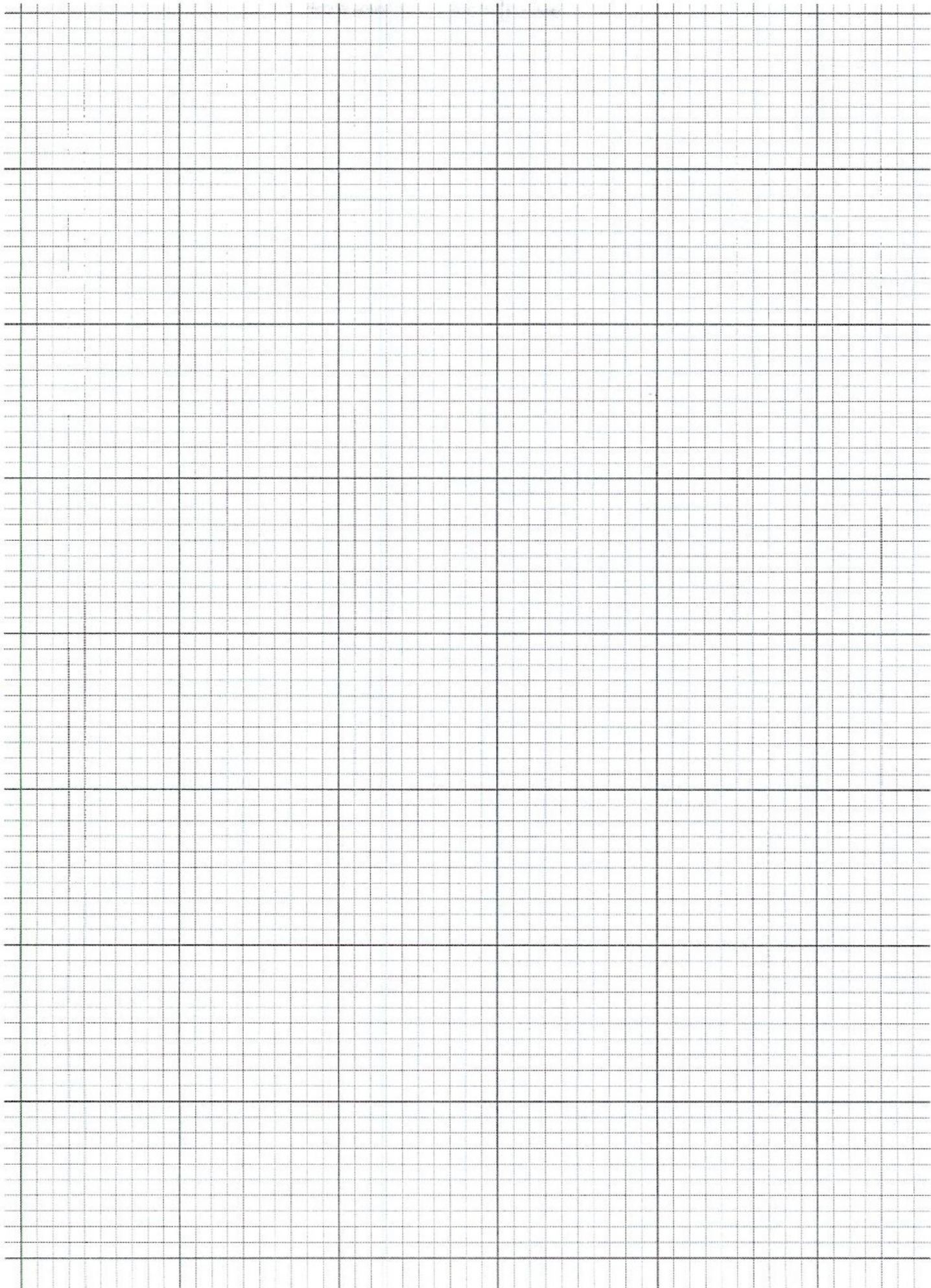
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$$(BC)^2 = (AB)^2 + (AC)^2 + 2(AB)(AD)$$

$$(6)^2 = (4)^2 + (3)^2 + 2(4)(AD)$$

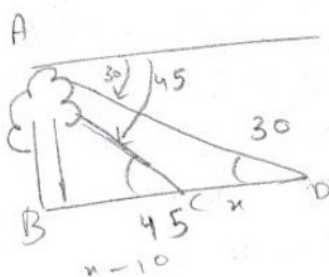
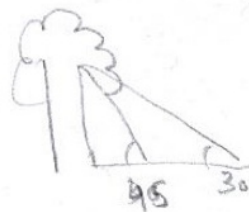
$$36 = 14 + 9 + 8(\overline{AD})$$

$$36 - 14 - 9 = 8(\overline{AD})$$

$$13 = 8(\overline{AD})$$

$$\overline{AD} = \frac{13}{8}$$

$$\therefore \overline{AD} = 1.6 \text{ cm h}$$



$$n = \frac{7a \times 2b}{a+b}$$

$$\frac{n}{7a} = \frac{2b}{a+b}$$

$$\frac{n+7a}{n-7a} = \frac{2b+a+b}{2b-a-b}$$

$$\frac{n+7a}{n-7a} = \frac{3b+a}{b-a}$$

$$\text{In } \triangle ABC,$$

$$\tan 45 = \frac{h}{n-10}$$

$$n-10 = h$$

$$h = n-10$$

$$\text{In } \triangle ABD,$$

$$\tan 30 = \frac{h}{n+(n-10)}$$

$$A = \frac{1}{2} r^2 \theta$$

$$= \frac{1}{2} (3)^2 \times \frac{\pi}{3}$$

$$= \frac{1}{2} \times 9 \times \frac{\pi}{3}$$

$$\frac{n}{7b} = \frac{2a}{a+b}$$

$$\tan 30 = \frac{n-10}{n+n-10}$$

$$(7+5w+5w^2)^2$$

$$(7+5(w+w^2))^2$$

$$\frac{n+7b}{n-7b} = \frac{2a+a+b}{2a-a-b}$$

$$\tan 30 = \frac{n-10}{2n-10}$$

$$(7-5)^2$$

$$(2)^2 = 4$$

$$\frac{n+7b}{n-7a} = \frac{3a+b}{a-b}$$

$$(2n-10)(\tan 30) = n-10$$

$$2n \tan 30 - 10 \tan 30 = n - 10$$

$$2n \tan 30 - n = -10 + 10 \tan 30$$

$$\frac{3b+a}{b-a} + \frac{3a+b}{a-b}$$

$$\times (2 \tan 30 - 1) = -10 + 10 \tan 30$$

$$\frac{3b+a}{b-a} - \frac{3a+b}{b-a}$$

$$3b+a - 3a-b$$

$$= \frac{-10 + 10 \tan 30}{2 \tan 30 - 1}$$

$$x = -27.32$$

$$\frac{3b+a}{b-a} - (b-a)$$